

# Numerical Simulation of Electrophotography Processes



**Hiroyuki Kawamoto**  
**Waseda University, Tokyo**

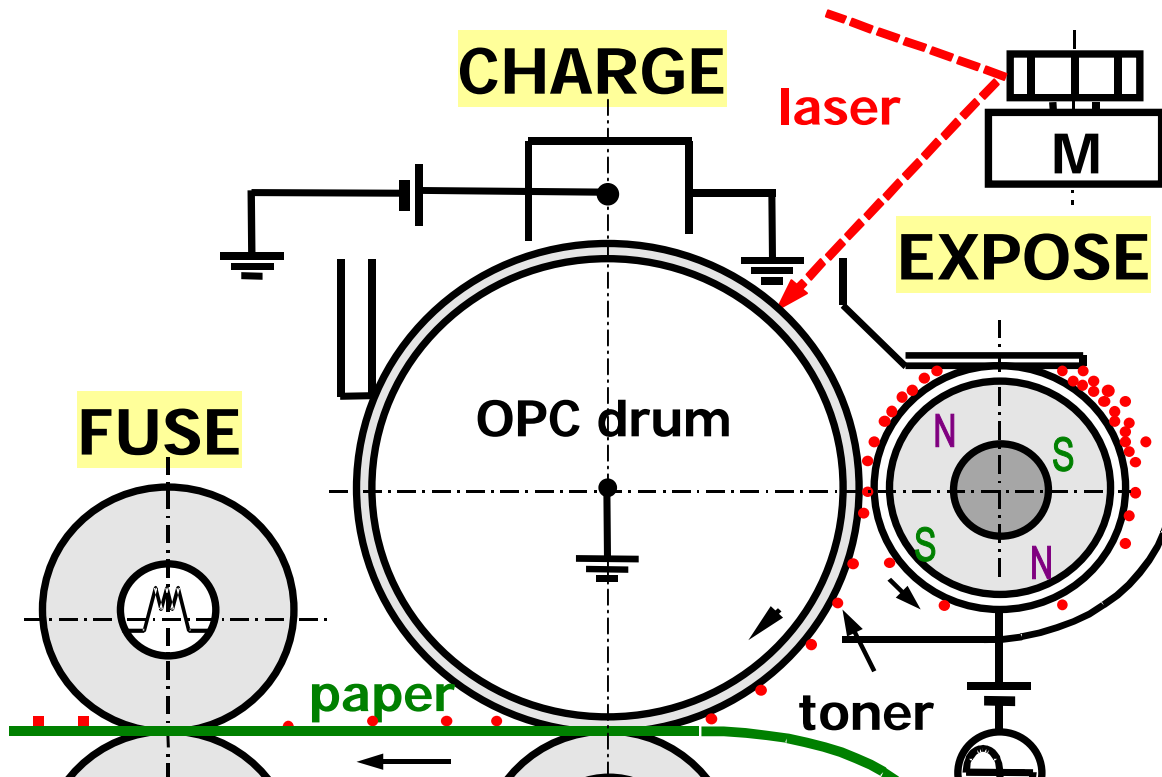
# Outline

**Overview of the recent progress of simulation technology for the development of electrophotography processes**

**- especially developed in Japan**

**Promotion of simulation technology and education of young engineers in Japan**

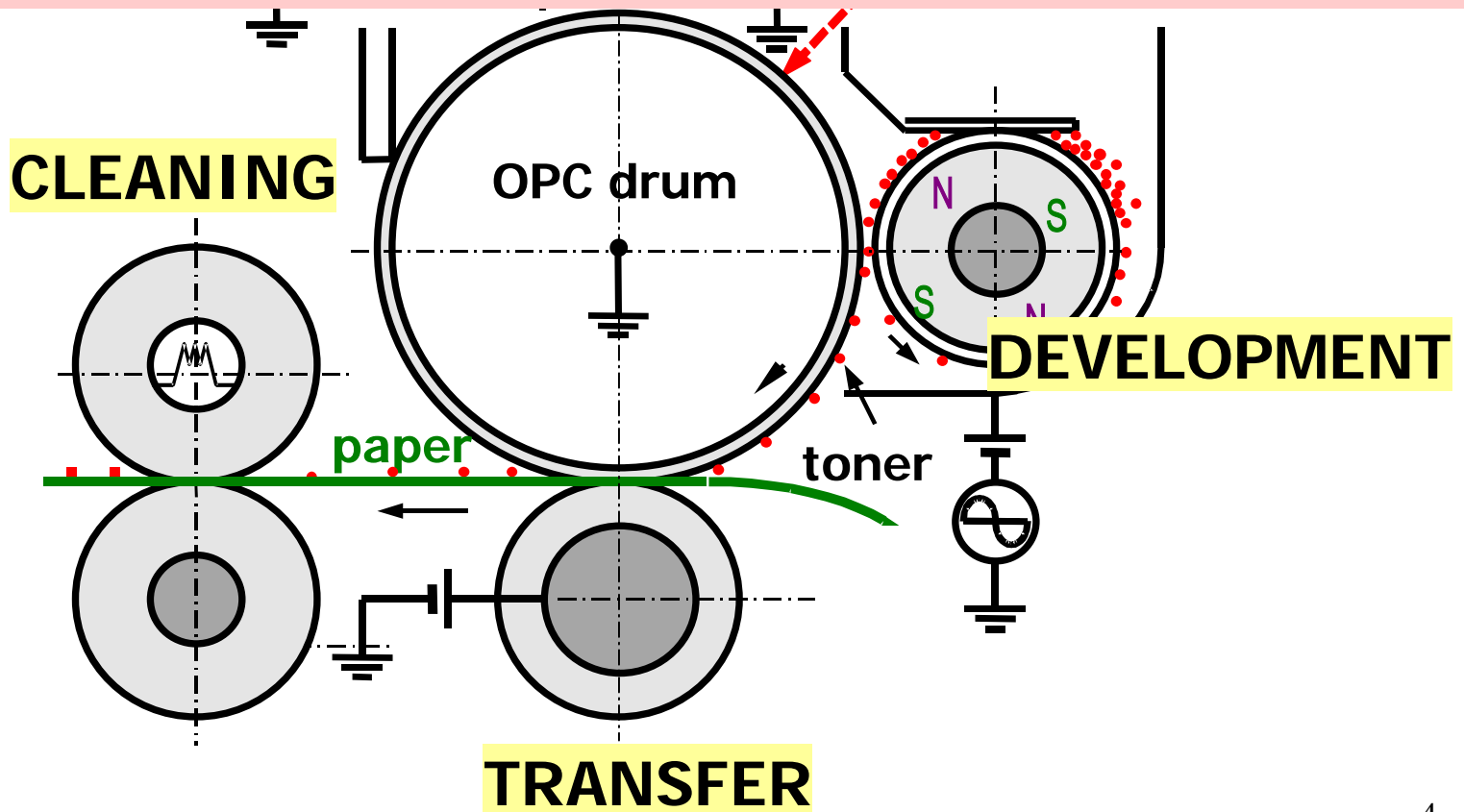
# Charging, Exposure and Fusing Systems



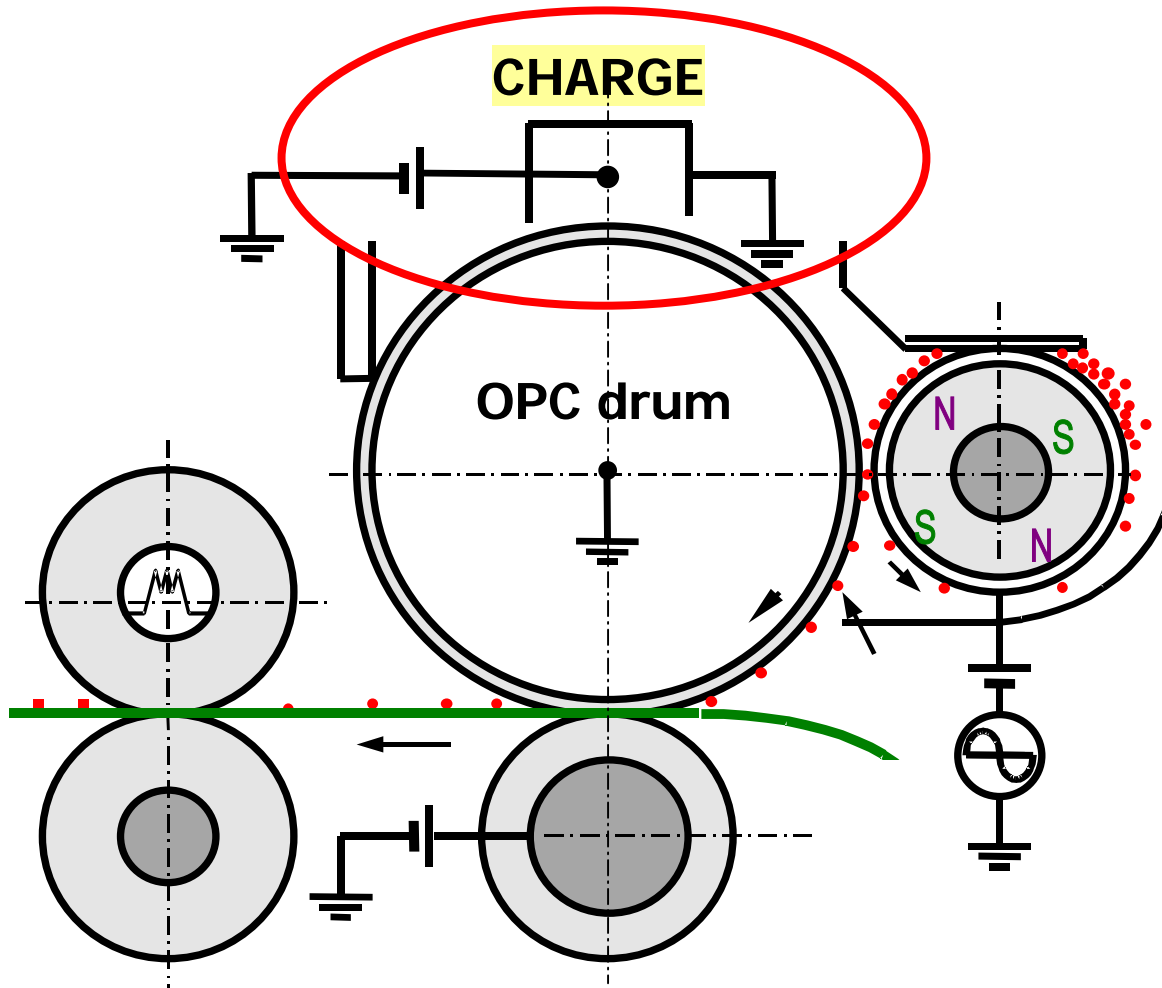
- based on the **mechanics of continuous media**
- formulated as a set of **multi-component, nonstationary, and nonlinear partial differential equations**
- numerically solved by the **iterative FEM or FDM**.

# Development, Transfer and Cleaning Systems

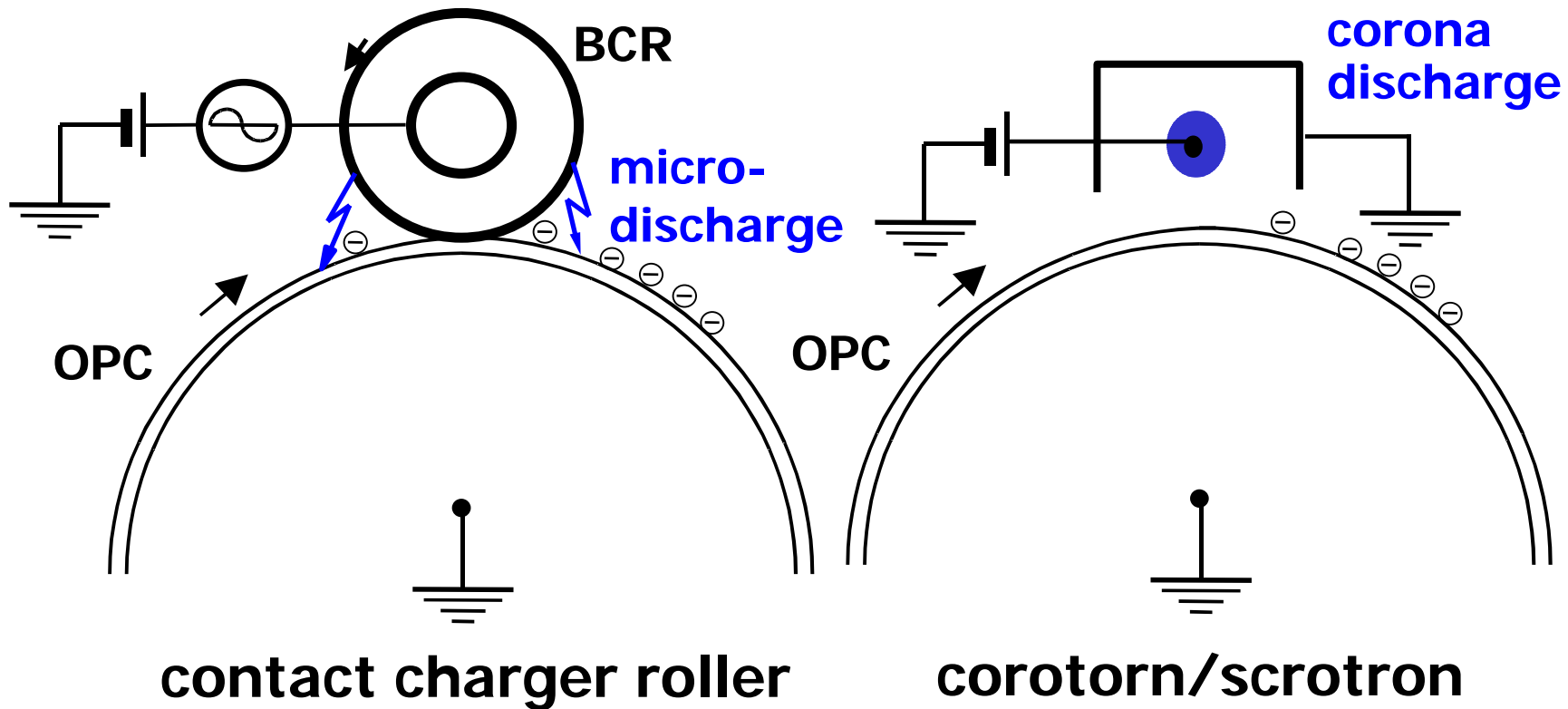
- dynamics of toner and/or carrier particles
- the discrete element method (DEM)
- direct observation with a high-speed microscope camera



# 1. Charging



# Charging Devices

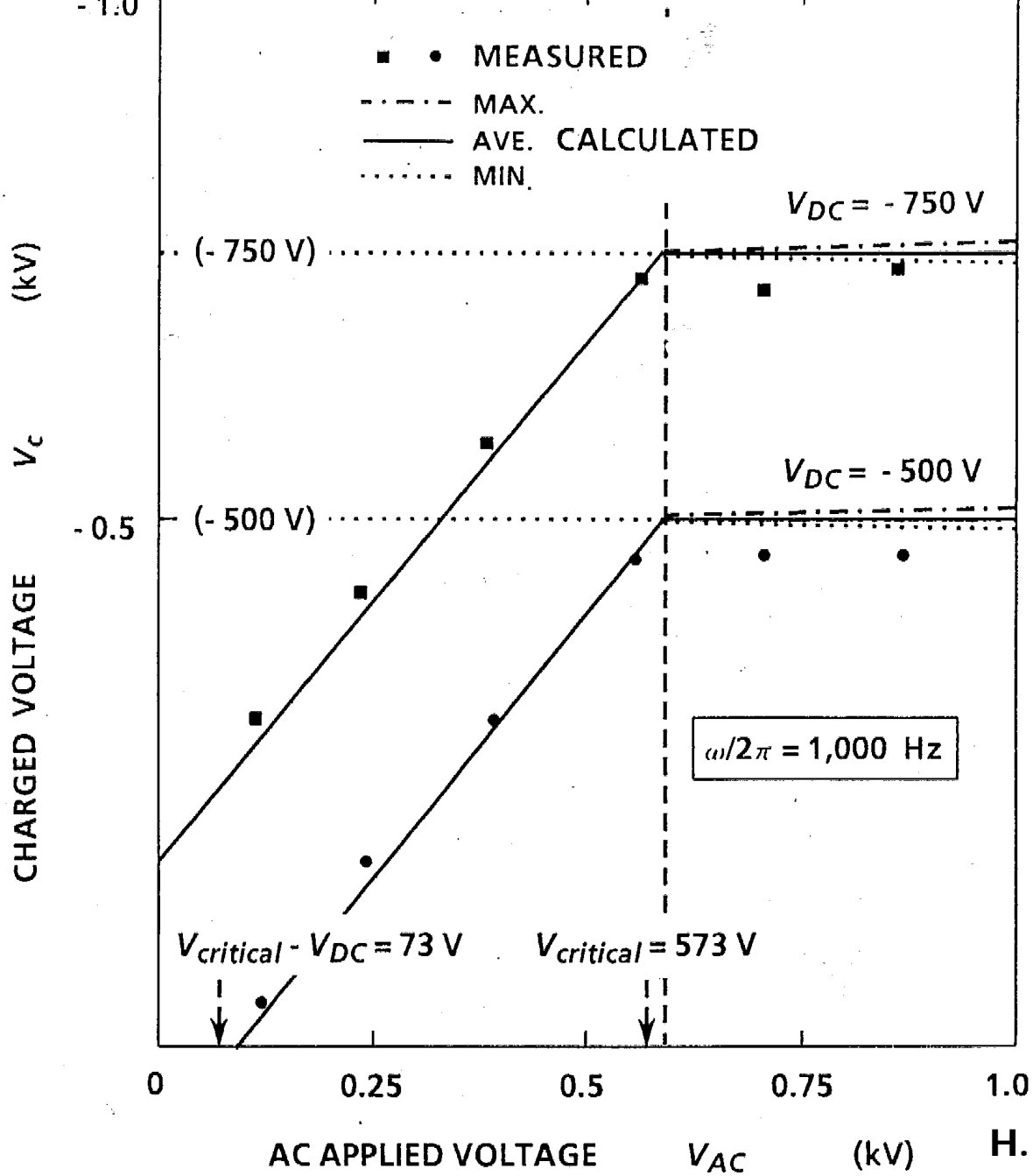


# Modeling of Contact Charging (one-dimensional analytical)

charged voltage  $V_c(t) = \frac{q(t)}{\epsilon_0 \epsilon_r} \frac{d}{z(t)}$

• charge density  $q(t + \Delta t) = \frac{\epsilon_0 \epsilon_r}{d} \left\{ V_a(t) - \frac{d + z(t) \epsilon_r}{z(t) \epsilon_r} V_{th}(t) \right\}$

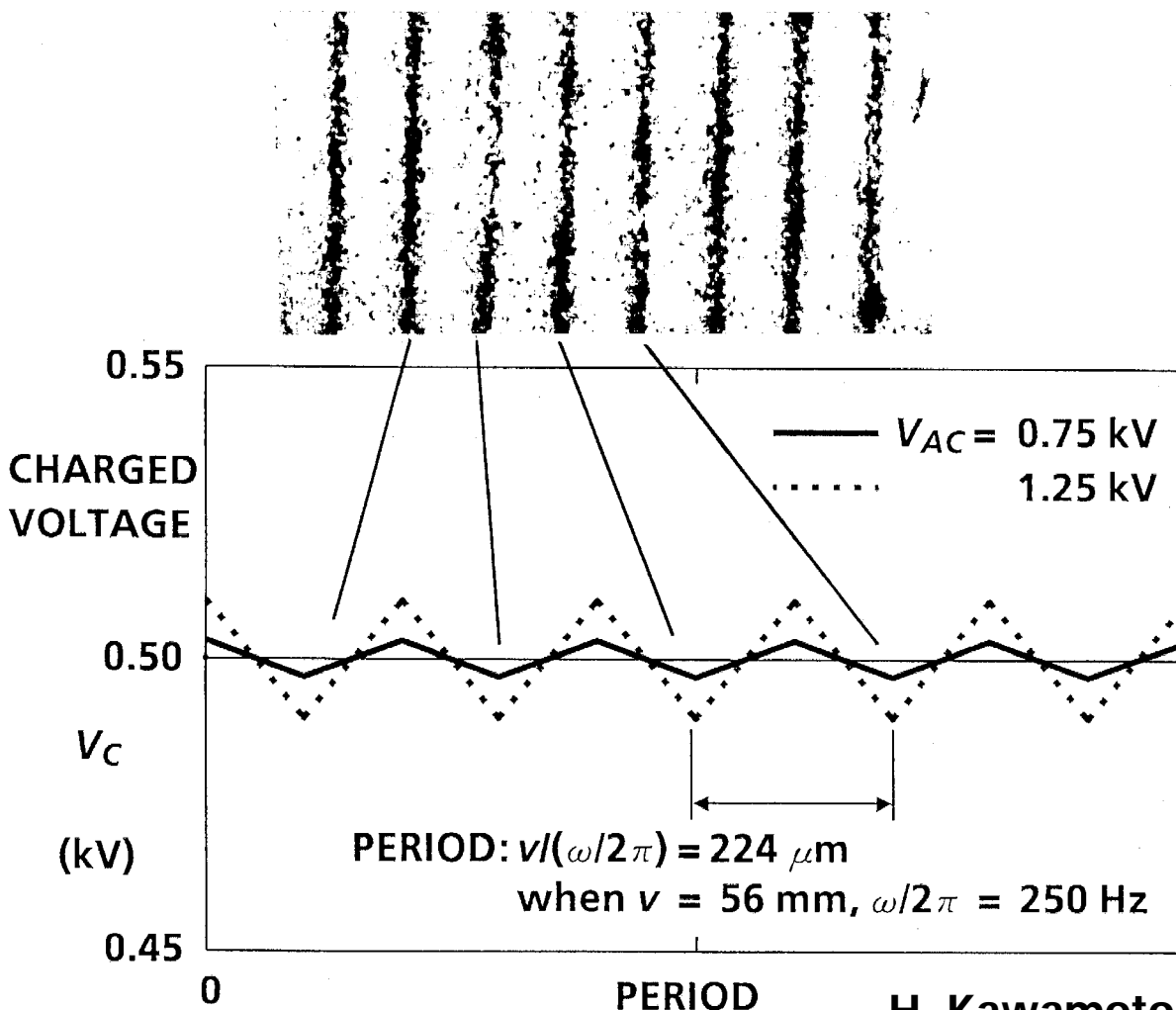
Micro discharge takes place  
when (gap voltage) > (Paschen  $V_{th}$ )



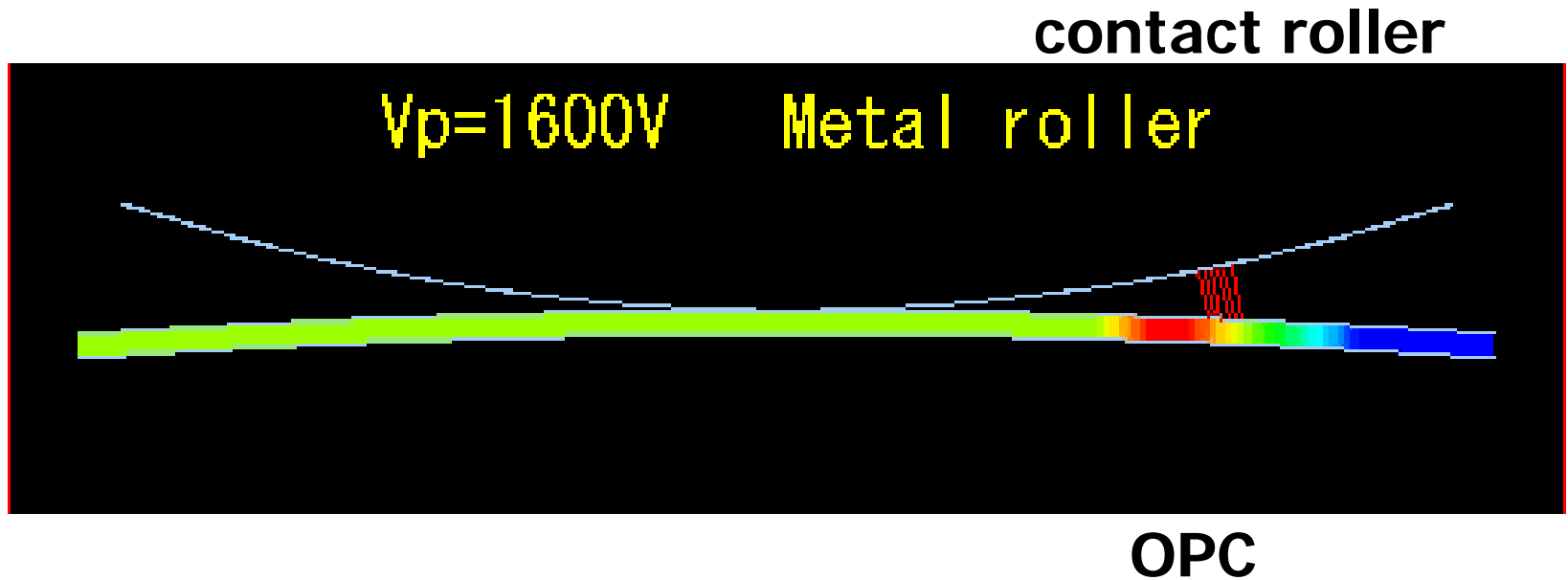
# Calculated and Measured Charging Characteristics



# Analysis of Strip Image Defect due to AC Voltage Application

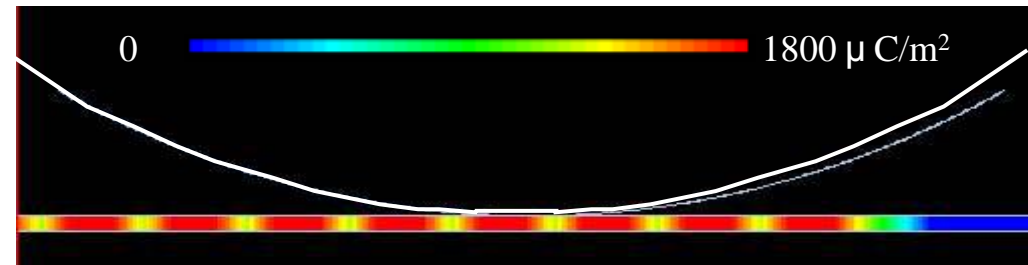
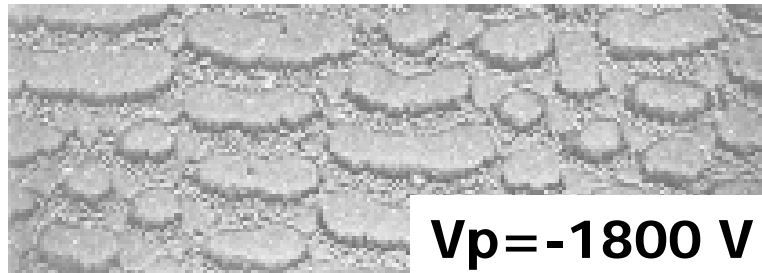
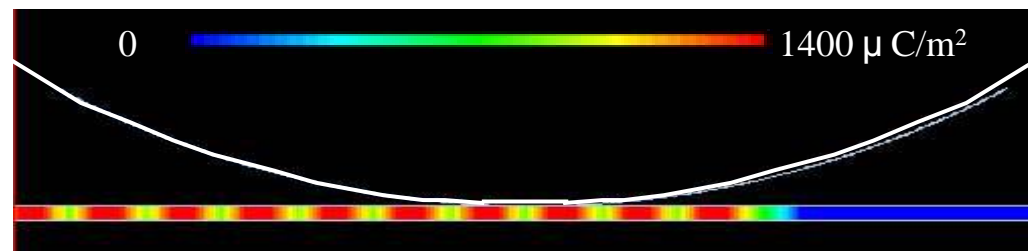
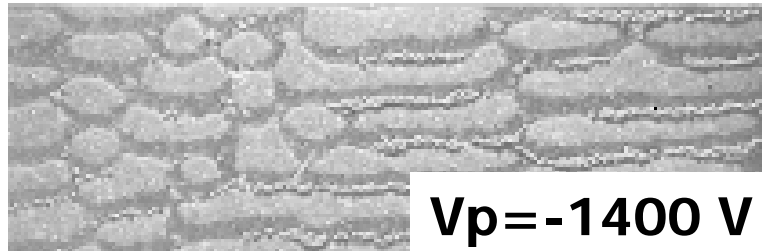
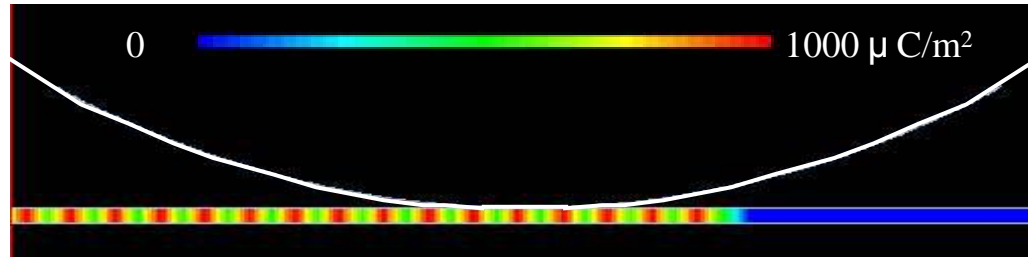
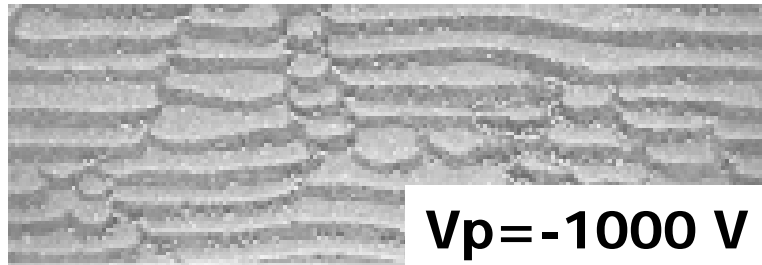


# Analysis of Image Defect due to DC Voltage Application



- expanded to 2D field
- circumferential transport of charge

# Analysis of Image Defect due to DC Voltage Application

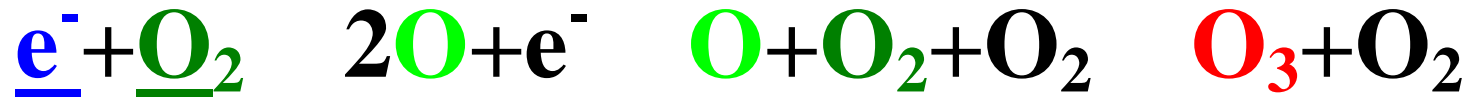


**observed image defect**

**calculated charge density**

# Plasma Ozone Synthesis

## Ozone Synthesis

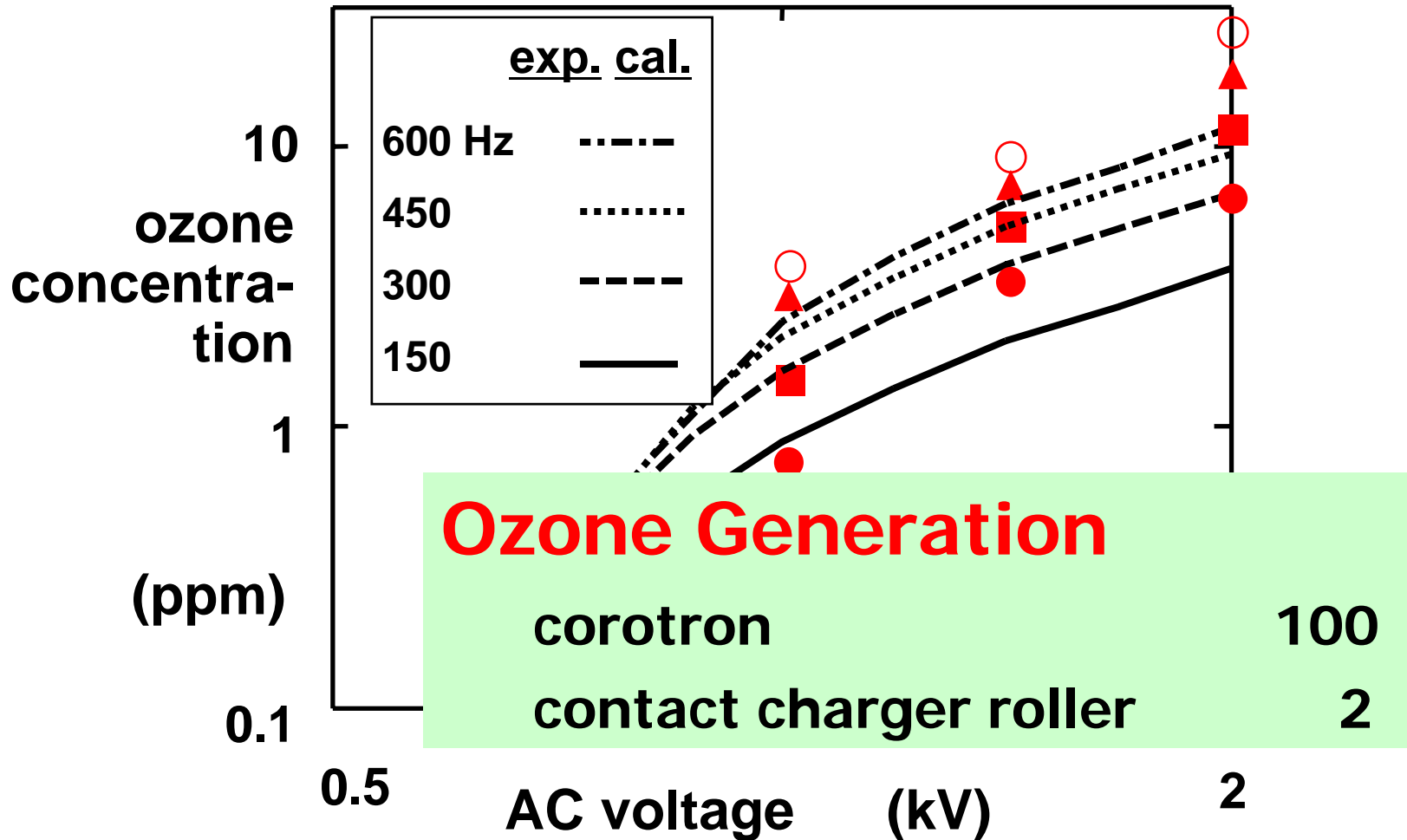


## Plasma Reaction Rate

$$S = 2\pi \int_{r_0}^R K_r n_e n_o r dr \quad (O_3/sec)$$

- based on Townsend theory

# Measured and Calculated Ozone Concentration



# Modeling of Corona Charging

conservation of charges

$$\frac{\partial n_p}{\partial t} + \text{div} \left( \mu_p \mathbf{E} n_p \right) = -R_e n_p n_n$$

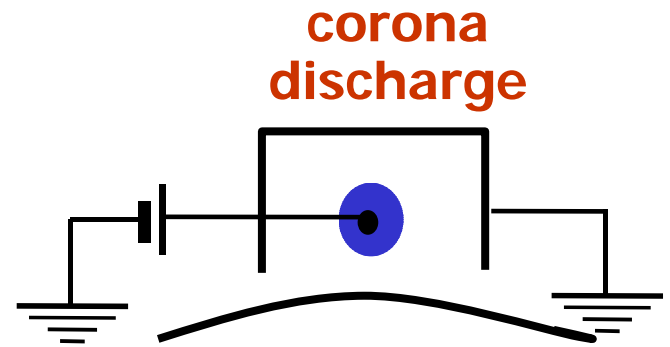
$$\frac{\partial n_n}{\partial t} + \text{div} \left( -\mu_n \mathbf{E} n_n \right) = -R_e n_p n_n$$

Poisson's equation

$$\text{div} \left( \varepsilon \mathbf{E} \right) = e \left( n_p - n_n \right)$$

boundary condition

$$E = E_{p0} \text{ (threshold of corona onset) at wire}$$

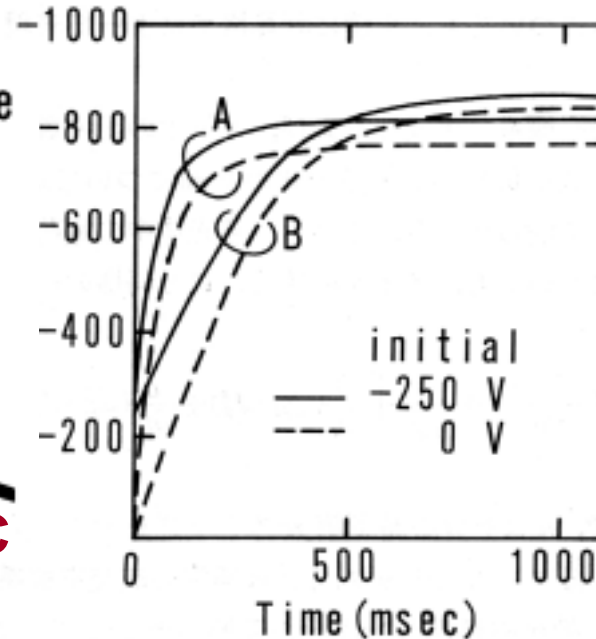
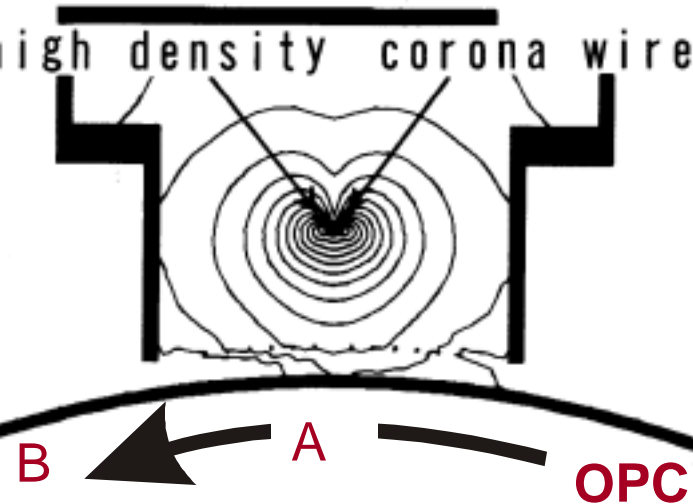
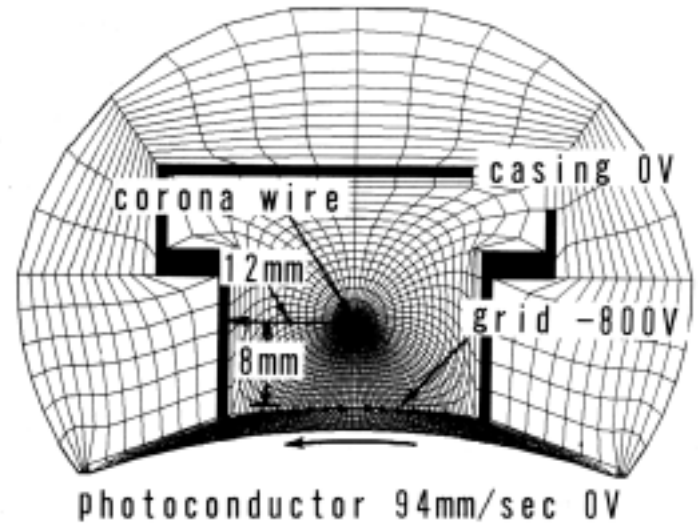


# Numerical Result

effects of rotation and resistivity of OPC

$$\mathbf{J}_p = \sigma \mathbf{E} + \rho \mathbf{v}_0$$

$$\frac{\partial \rho}{\partial t} + \text{div } \mathbf{J}_p = 0$$



**initial 0 V**

cal. - 863 V

exp. - 900 V

**initial - 250 V**

cal. - 886 V

exp. - 925 V

# Flow Analysis of Ionic Wind

## Discharge Field (2D, unipolar)

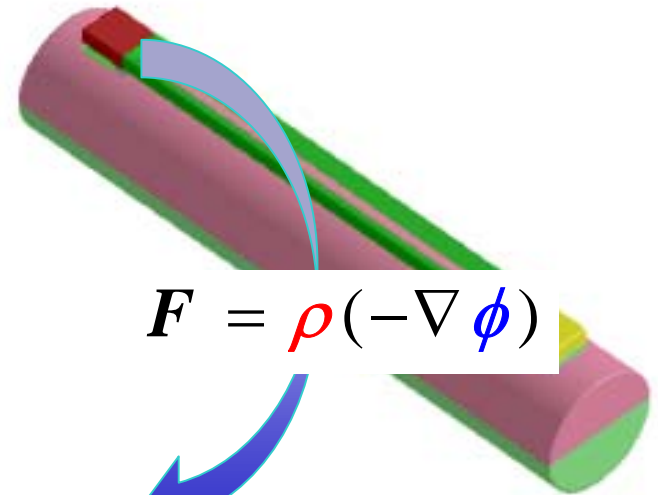
$$\frac{\partial \rho}{\partial t} + \nabla \left( \mu \rho (-\nabla \phi) \right) = 0$$

$$\nabla \left( \varepsilon (-\nabla \phi) \right) = \rho$$

## Aerodynamics (3D)

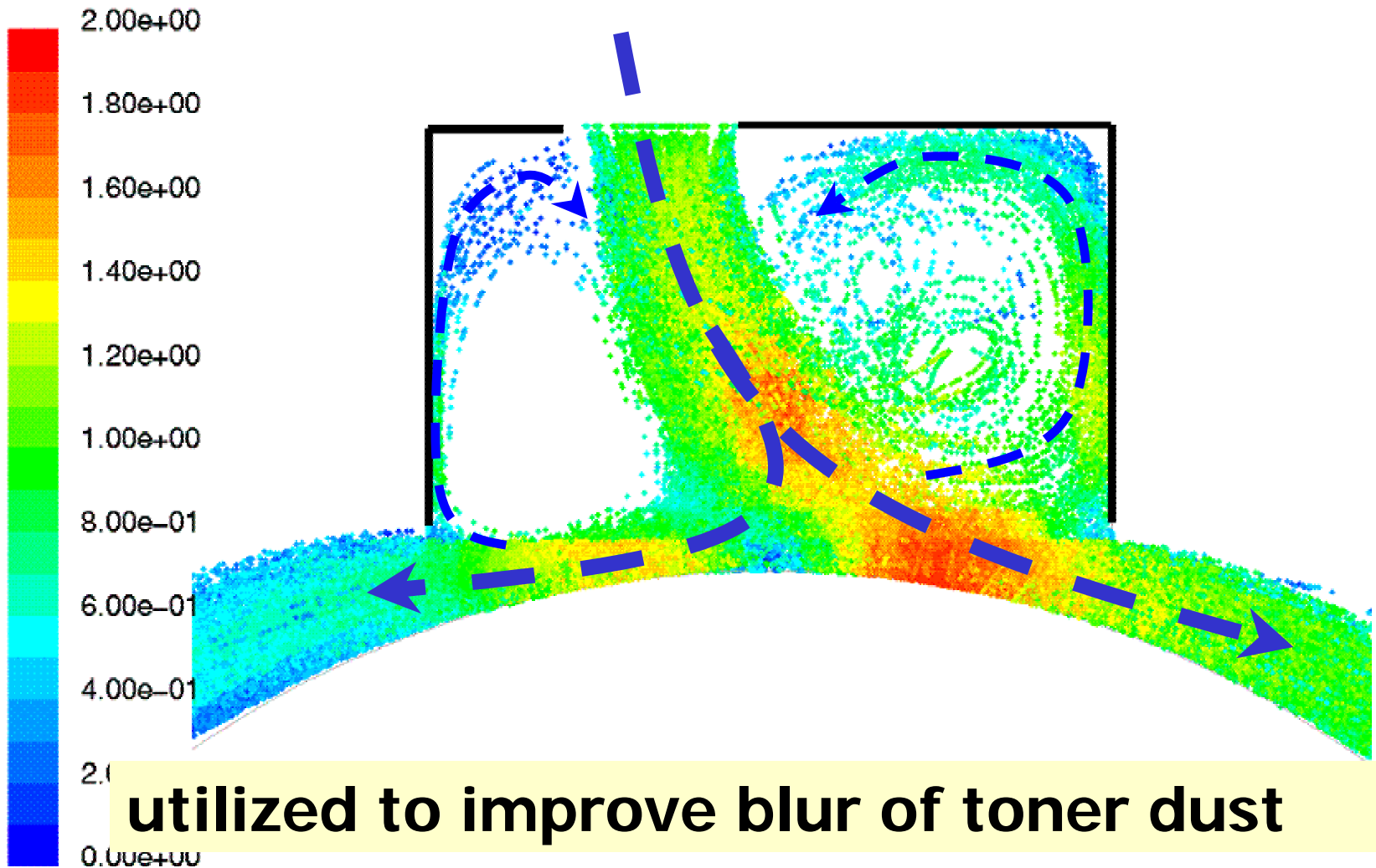
$$\frac{\partial \rho_g \mathbf{u}}{\partial t} + \rho_g (\mathbf{u} \cdot \nabla) \mathbf{u} = -\nabla p + \mu_g \Delta \mathbf{u} + \mathbf{F}$$

**Navier-Stokes**

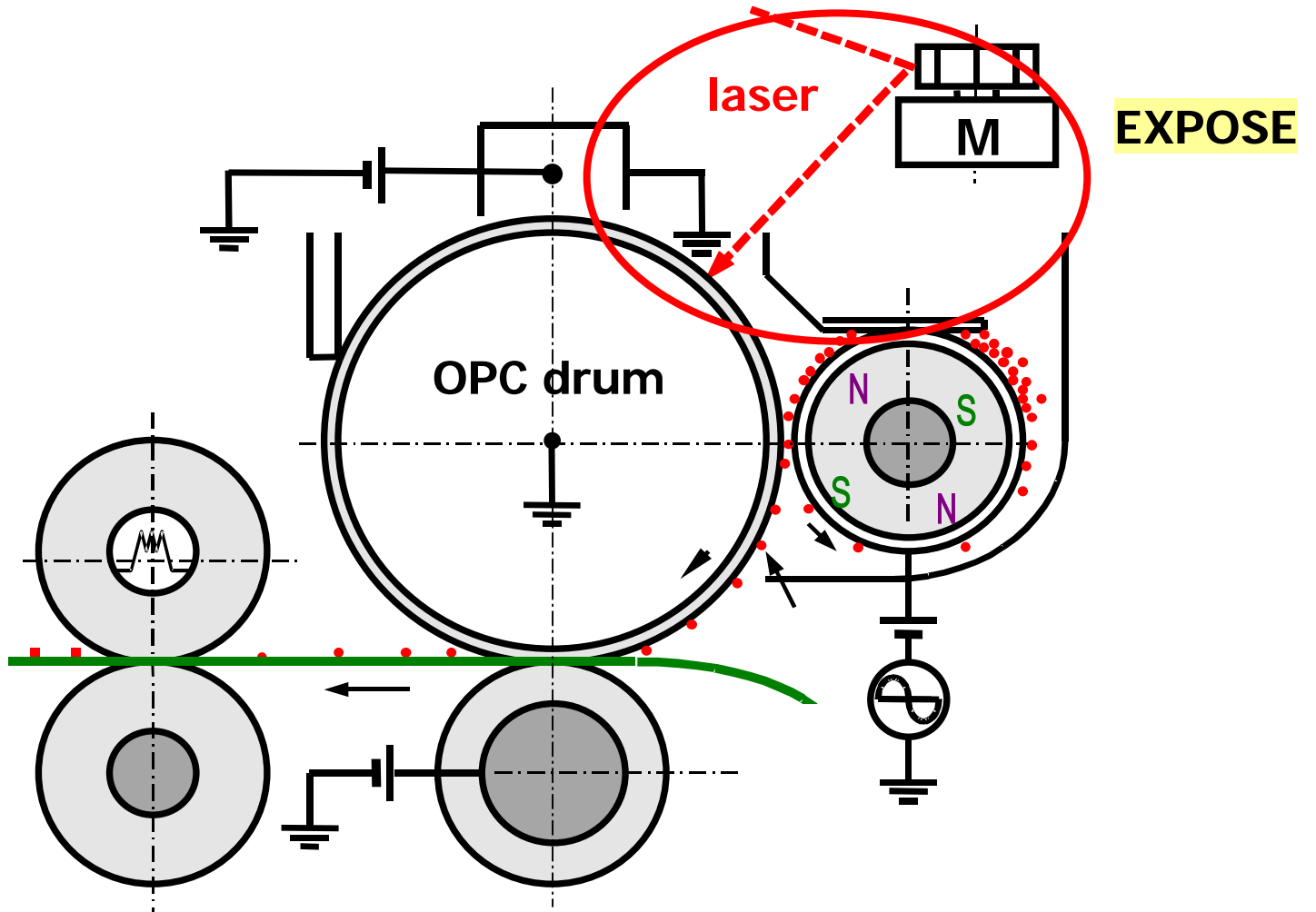




# Calculated Velocity Distribution



# 2. Exposure



# Formation of Latent Image (3D, time-dependent, 3-unknowns)

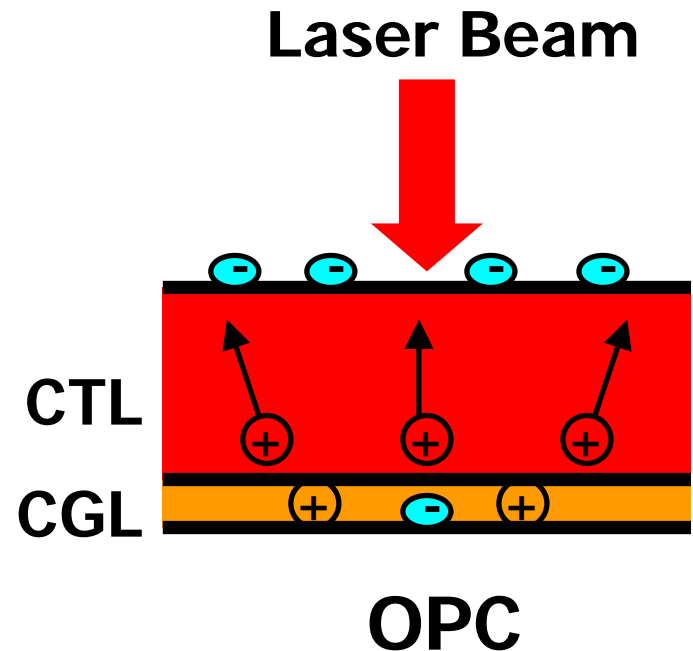
conservation of charges

$$\frac{\partial n_p}{\partial t} + \text{div}(\mu_p \mathbf{E} n_p) = \Gamma - R_e n_p n_n$$

$$\frac{\partial n_n}{\partial t} - \text{div}(\mu_n \mathbf{E} n_n) = \Gamma - R_e n_p n_n$$

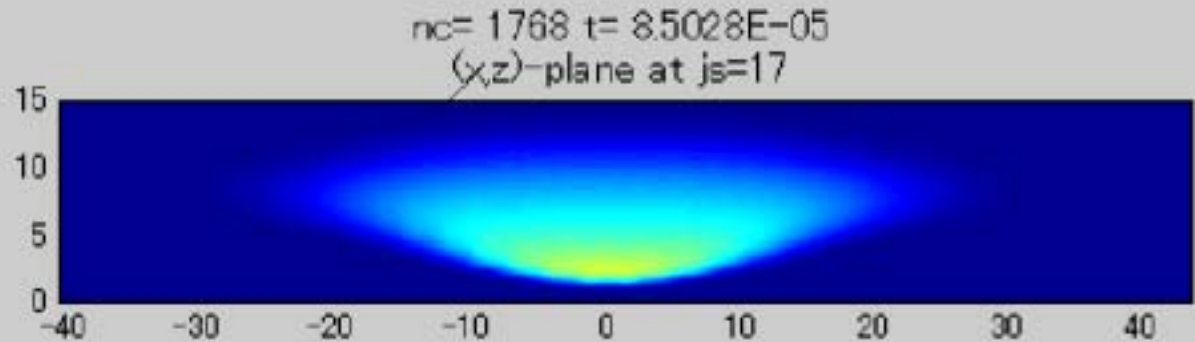
Poisson'Equation

$$\text{div}(\varepsilon \mathbf{E}) = e(n_p - n_n)$$



# Calculated Transient Charge Distribution

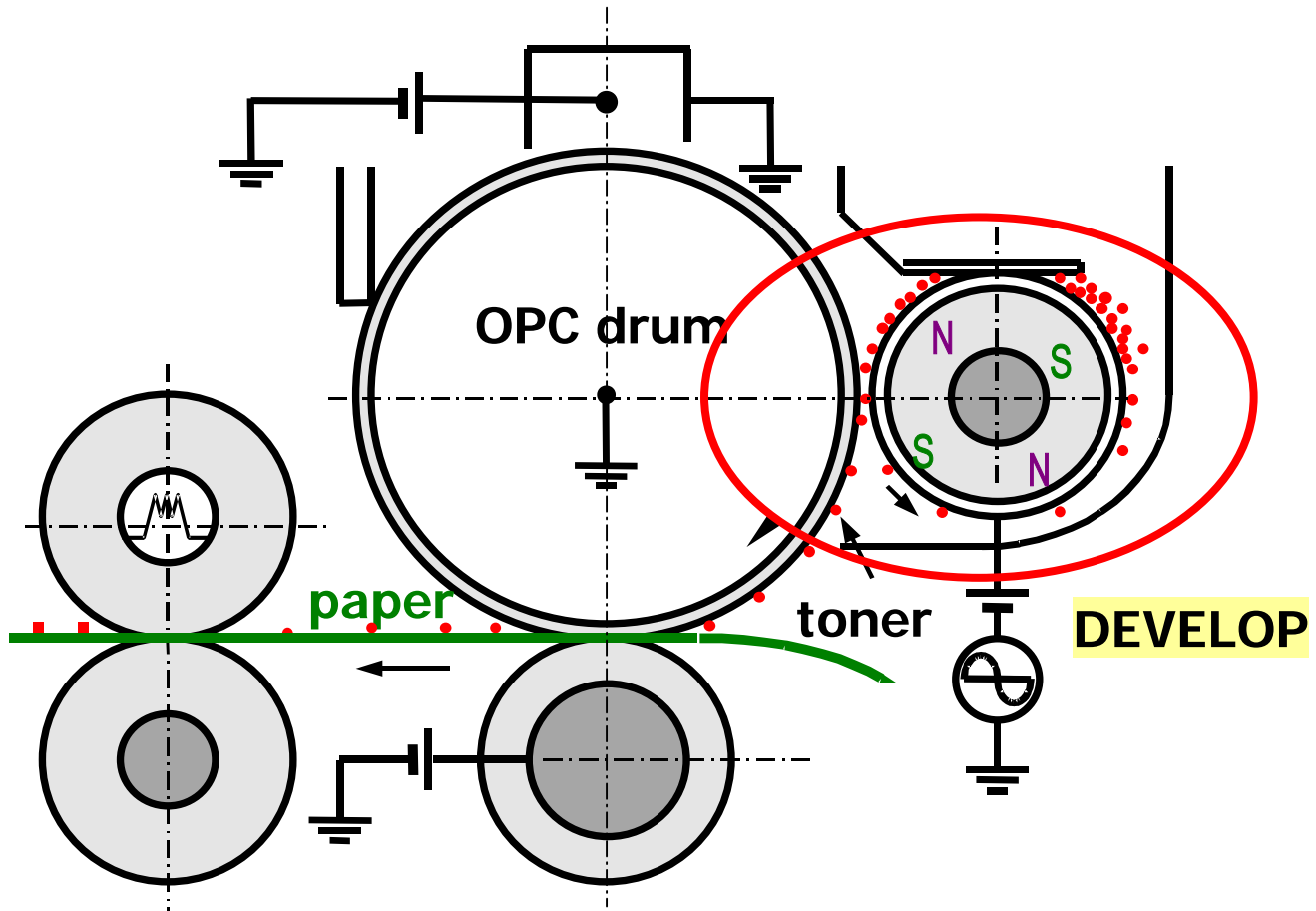
main scan



- Calculated field strength can predict threshold of development.
- Latent image created by an isolated dot spreads even if the thickness of OPC is  $10\ \mu\text{m}$ .
- Latent image created by one-by-one dot is suppressed by adjacent dots.

beam size:  $30\ \mu\text{m}$

# 3. Development



# Two Approaches for Toner/Carrier Dynamics

- Continuous Model

## Navier-Stokes

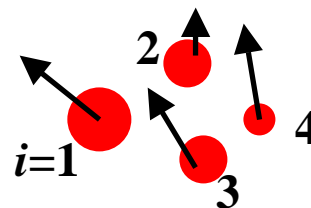
- (Hitachi Printing, Ricoh, Fuji Xerox, ---), 2000

- Discrete Model

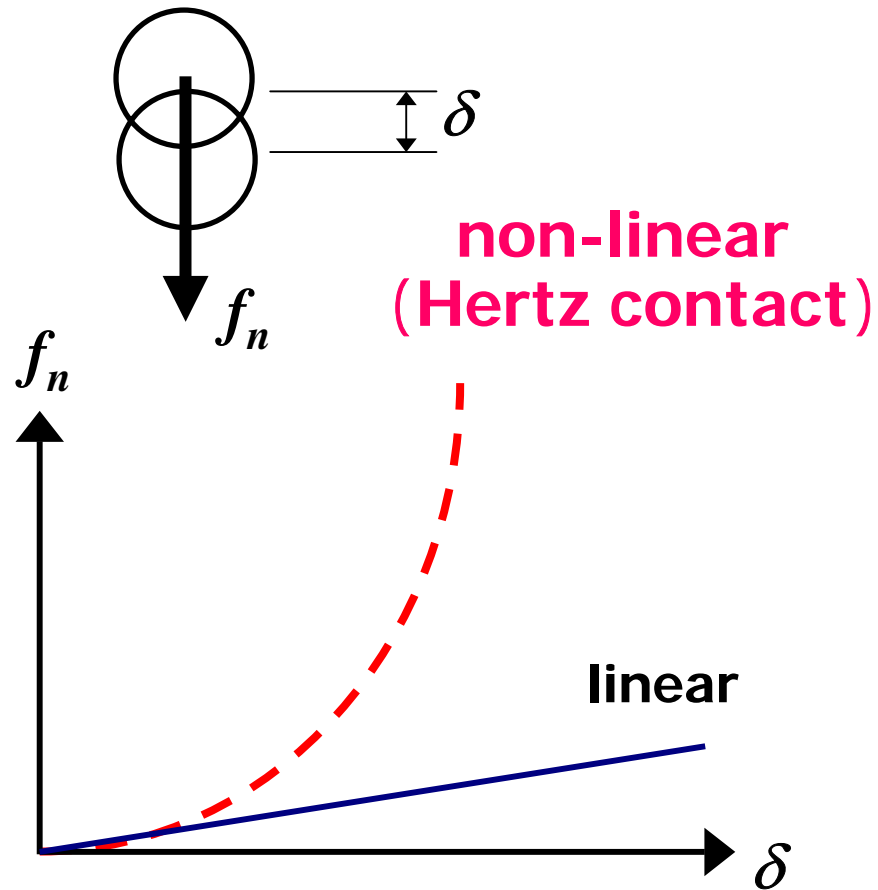
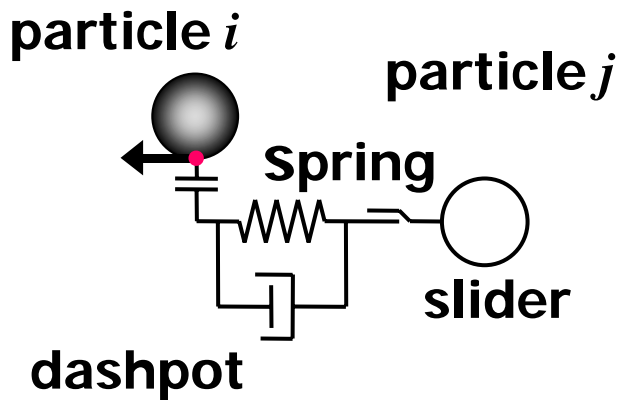
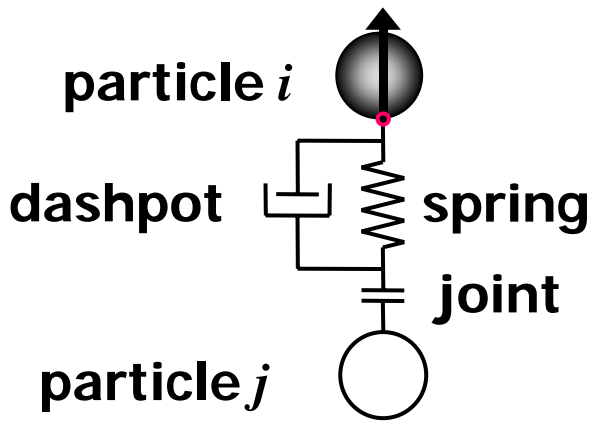
## Discrete Element Method (DEM)

$$m_i \ddot{\mathbf{x}}_i + \mathbf{c}_i \dot{\mathbf{x}}_i + \mathbf{k}_i \mathbf{x}_i = \mathbf{F}_{mechanical} + \mathbf{F}_{electrostatic} + \mathbf{F}_{magnetic} +$$

$$\mathbf{x} = (x, y, z, \theta_x, \theta_y, \theta_z)$$

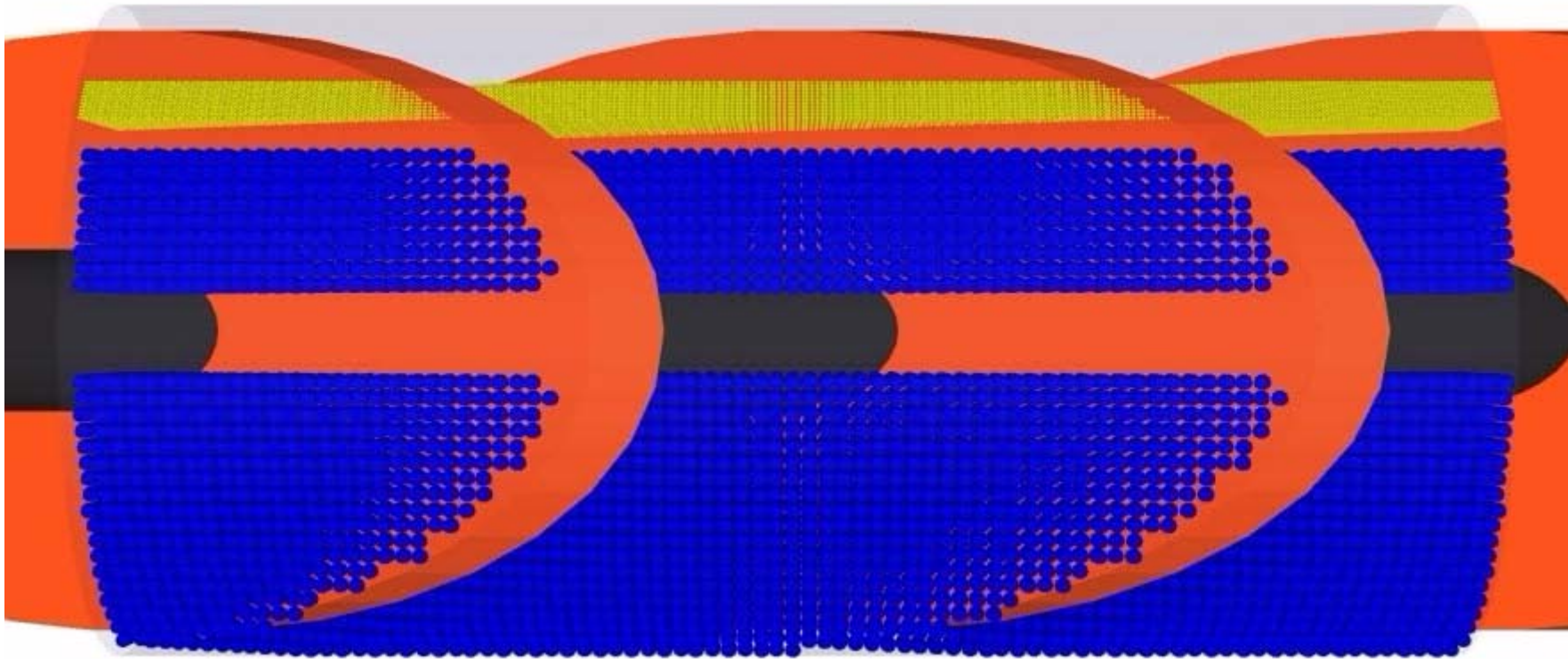


# Mechanical Interaction



Mechanical Interaction between Beads (Voigt model)

# Mixing of Toner and Carrier Particles in Auger





# Magnetic Interaction

- magnetic force

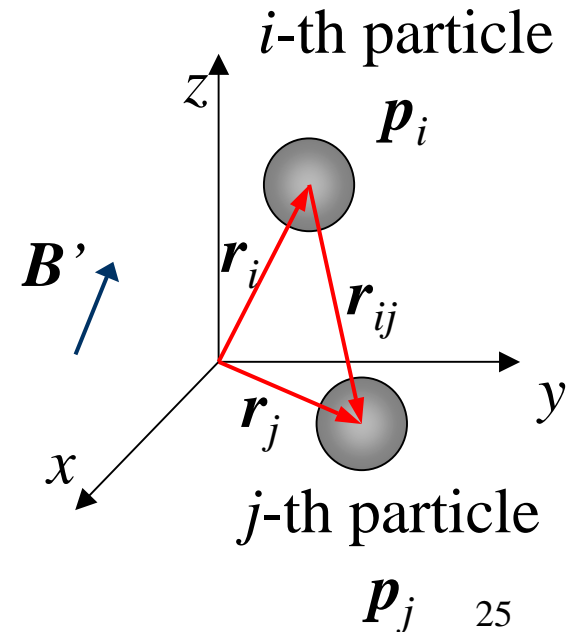
$$\mathbf{f}_{mj} = (\mathbf{p}_j \cdot \nabla) \mathbf{B}_j, \quad \mathbf{M}_{mj} = \mathbf{p}_j \times \mathbf{B}_j$$

- magnetic dipole moment

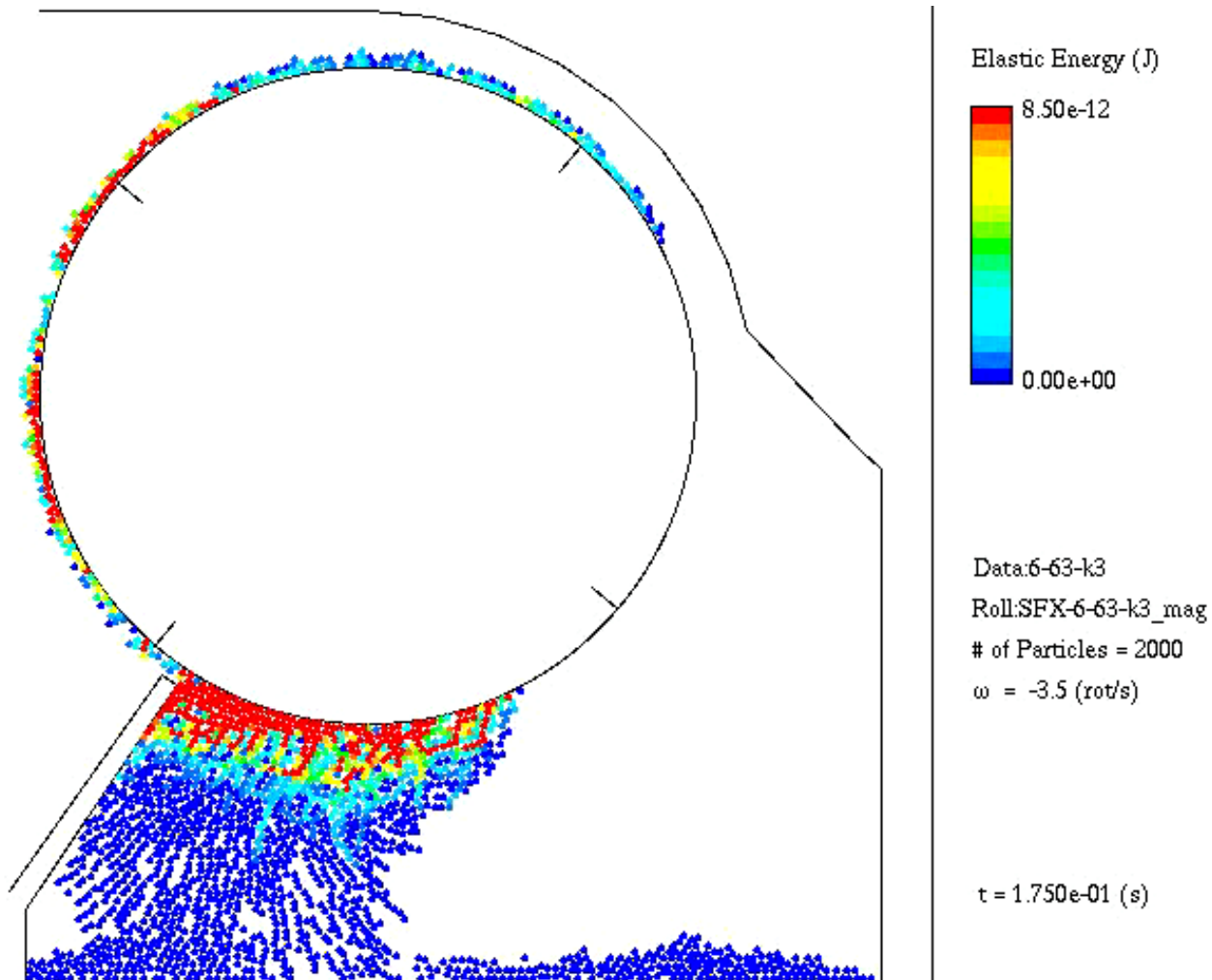
$$\mathbf{p}_j = \frac{4\pi}{\mu_0} \frac{\mu - 1}{\mu + 2} \frac{a_j^3}{8} \mathbf{B}_j', \quad \text{due to mag. roller}$$

$$+ \frac{\mu - 1}{\mu + 2} \frac{a_j^3}{8} \sum_{\substack{i=1 \\ j \neq i}}^N \left( \frac{3 \mathbf{p}_i \cdot \mathbf{r}_{ij}}{|\mathbf{r}_{ij}|^5} \mathbf{r}_{ij} - \frac{\mathbf{p}_i}{|\mathbf{r}_{ij}|^3} \right)$$

due to other particles



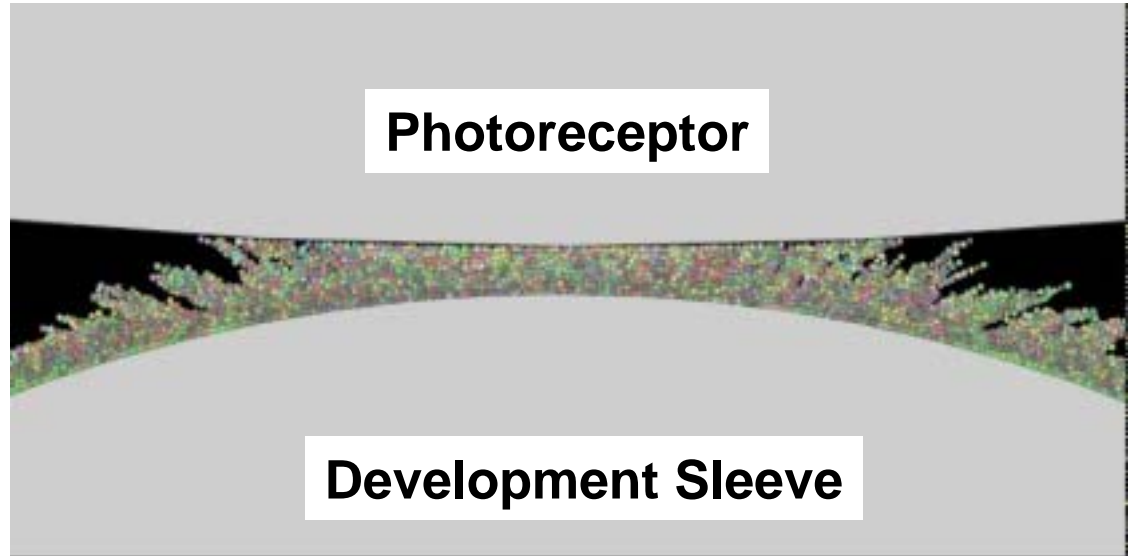
# Design of Magnetic Roller



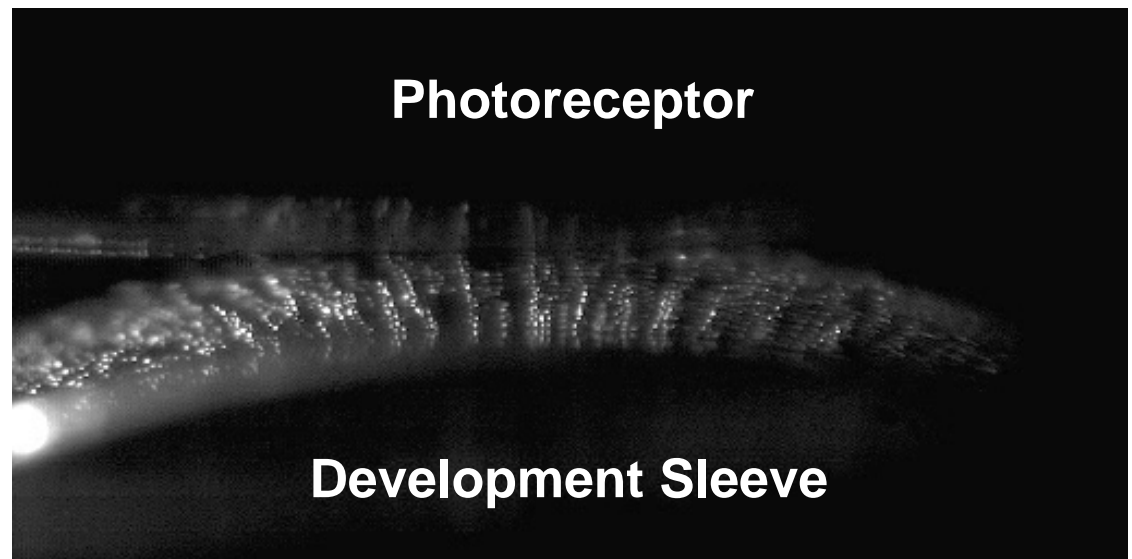
utilized to improve pole pattern of magnetic roller that can efficiently mix toner/carrier particles.

# Magnetic Brushes

**Simulation**



**Experiment**



# Two-Component Development

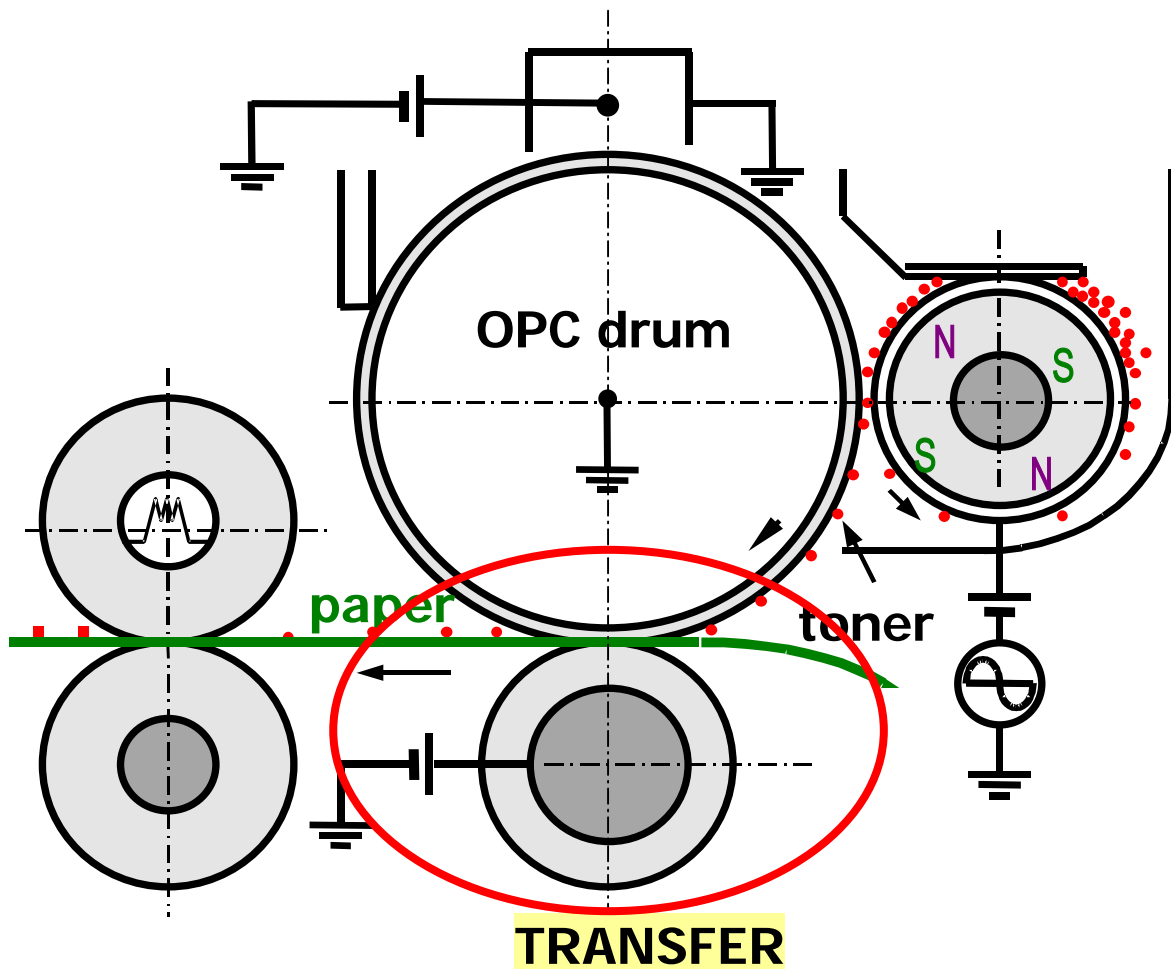


H. Mio (Kyoto Fine Particle Technology) 2007

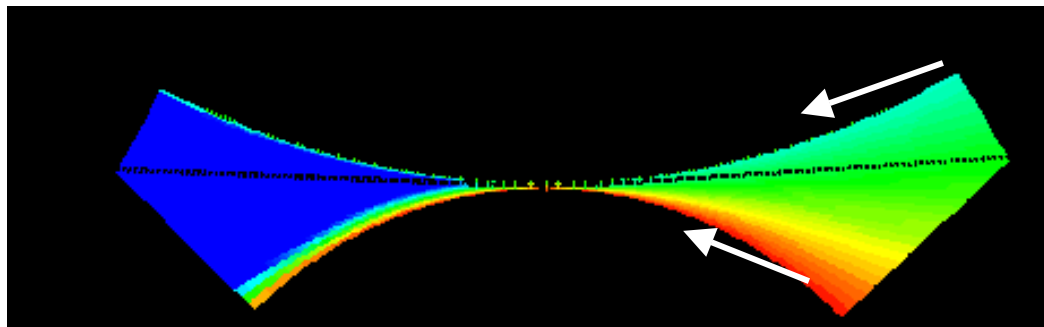
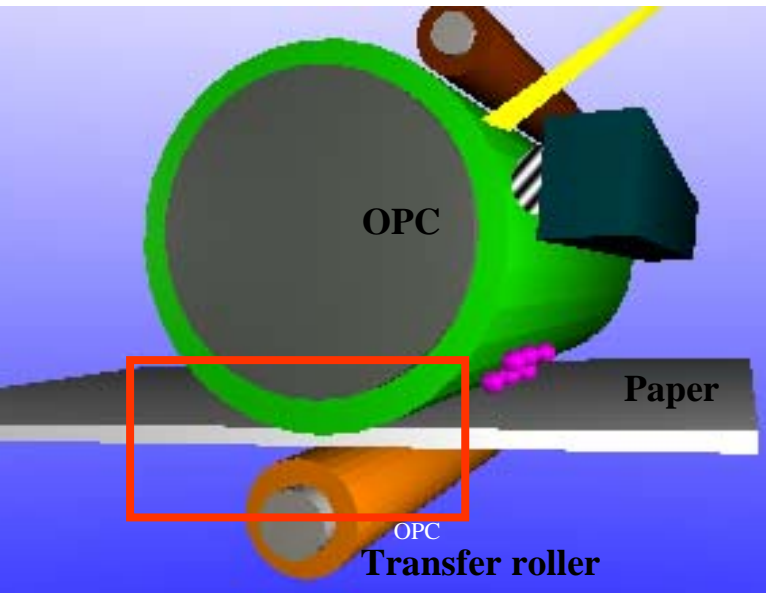
# Direct Observation of Development by High Speed Camera



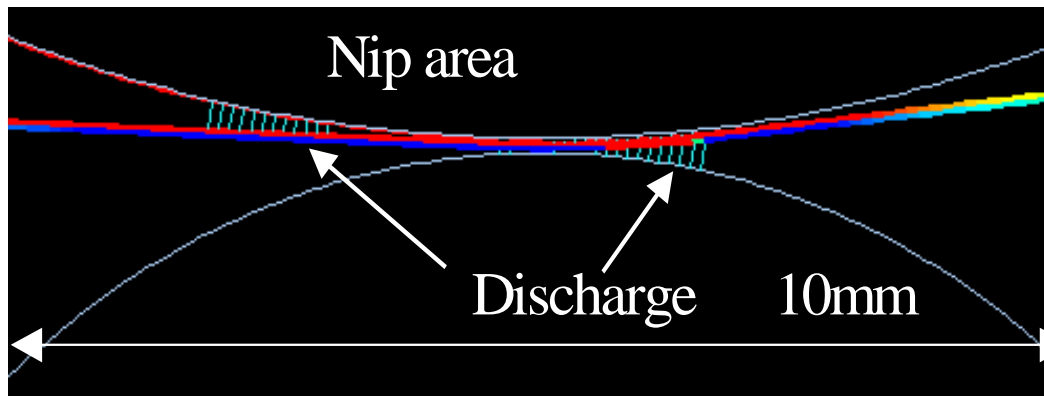
# 4. Transfer



# Electrostatic Field in Transfer Process

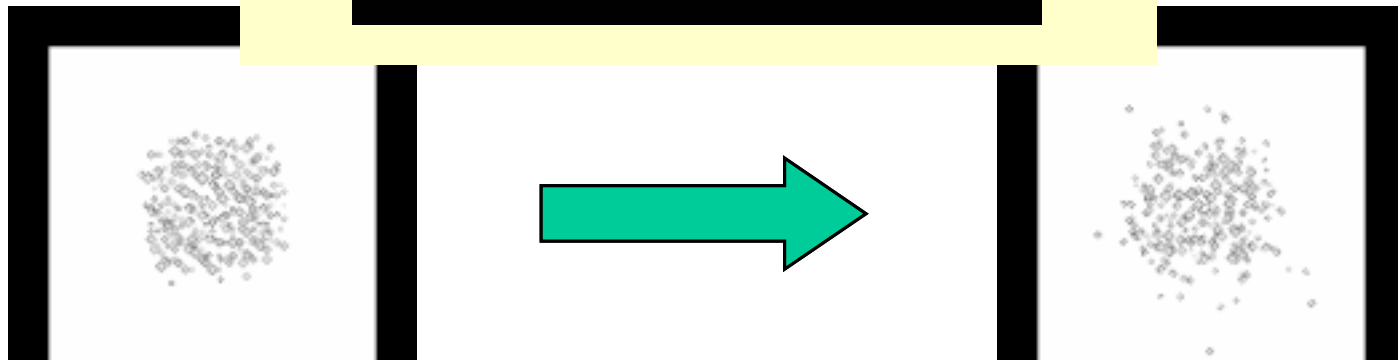
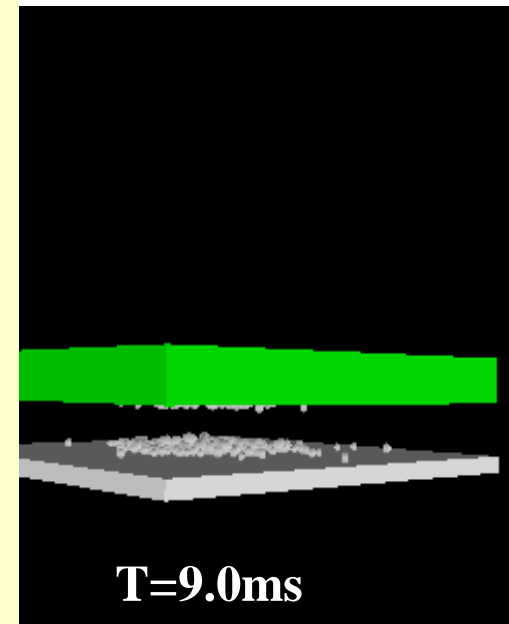
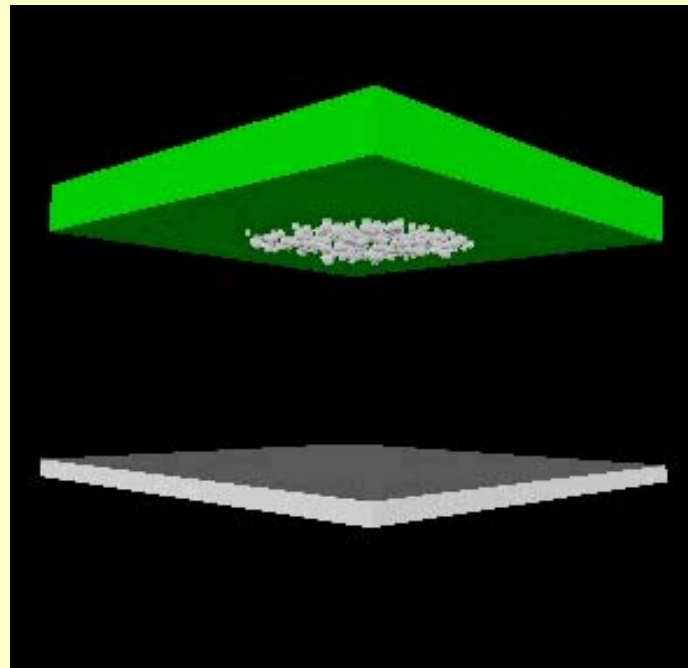
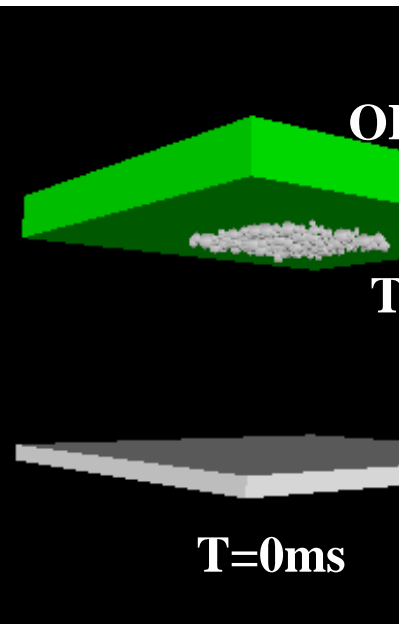


potential distribution



discharge

# Toner Dynamics in Roller Transfer System



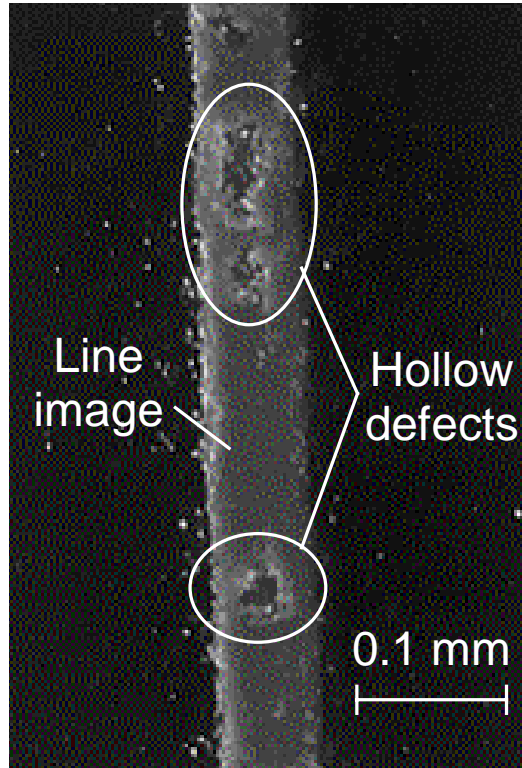
**Toner particles scatter due to electrical discharge.**

**on OPC**

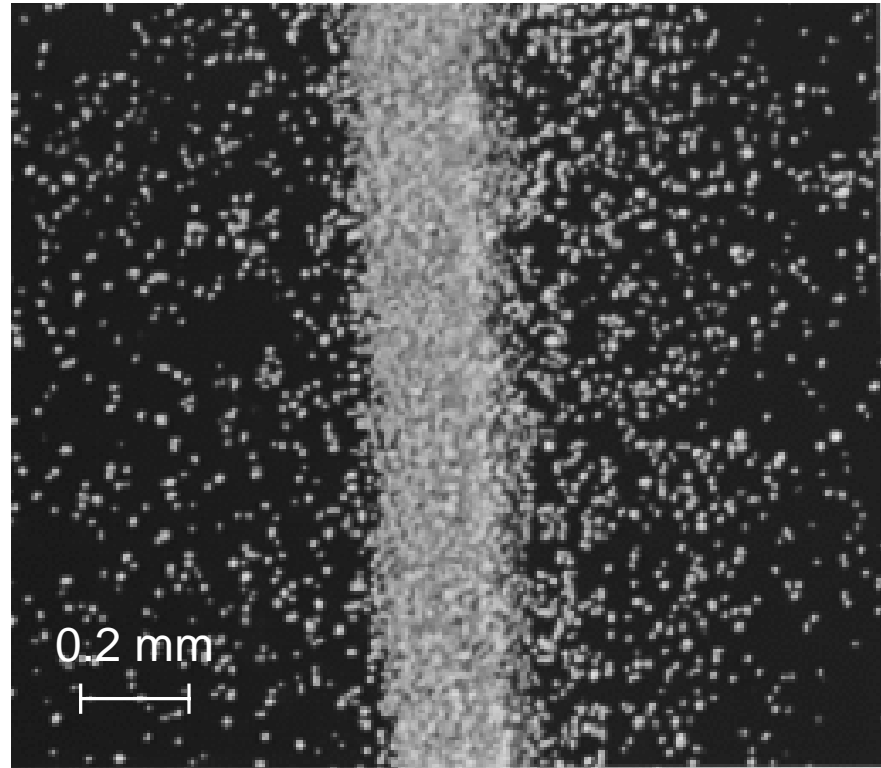
**on paper**



# Hollow Defect and Toner Scattering

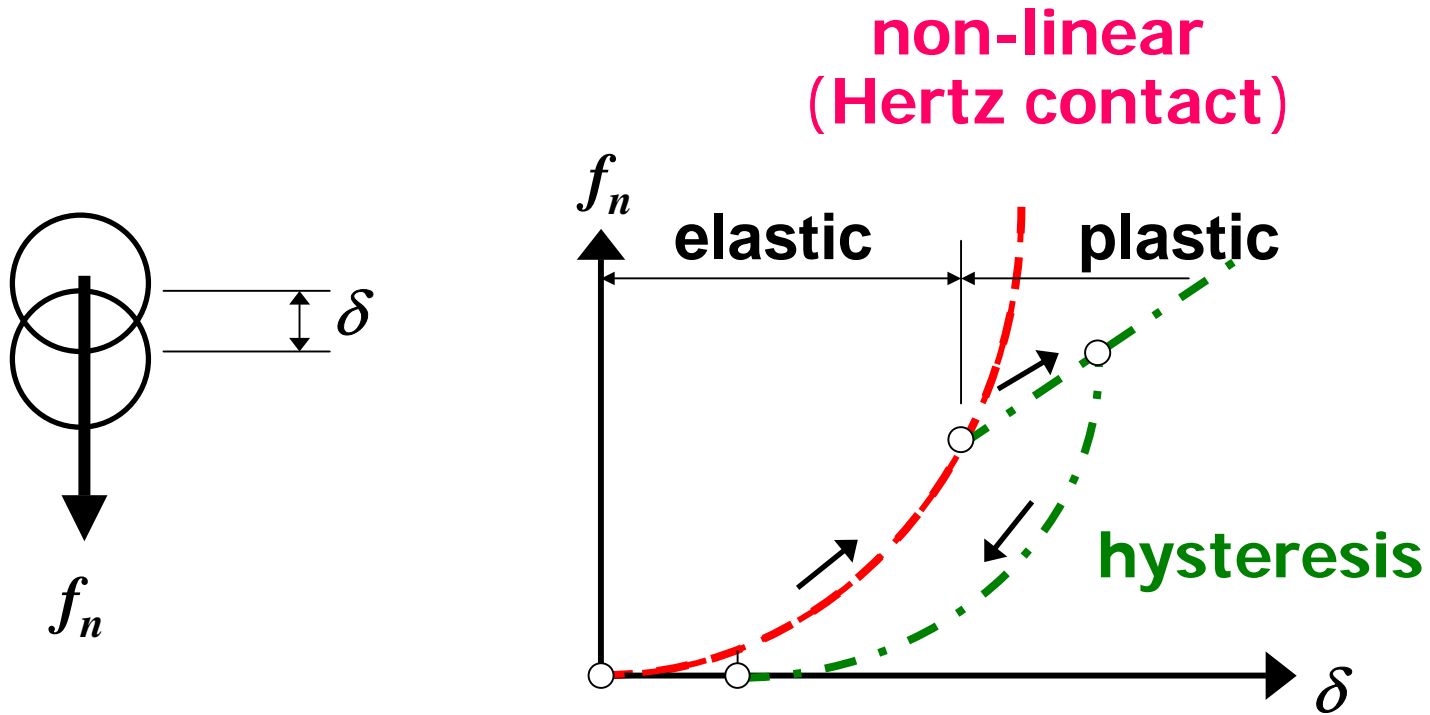


**hollow defect**

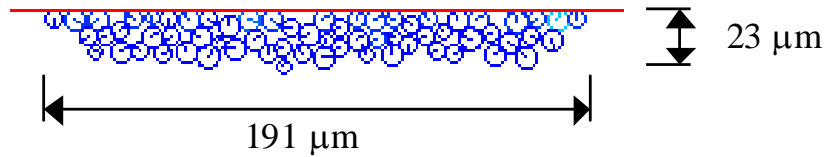


**toner scattering**

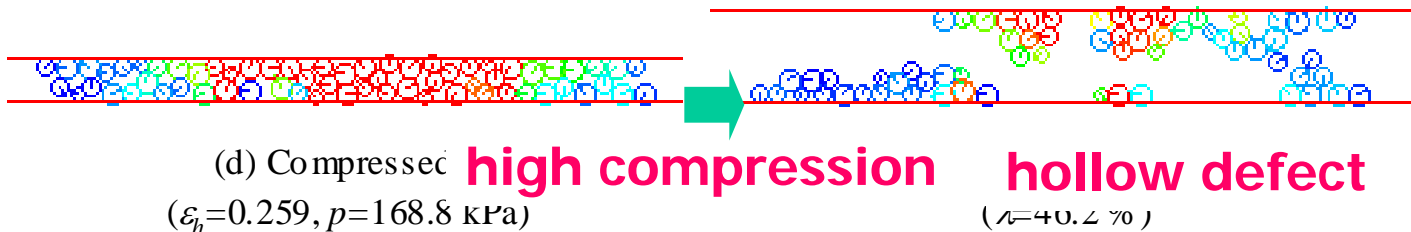
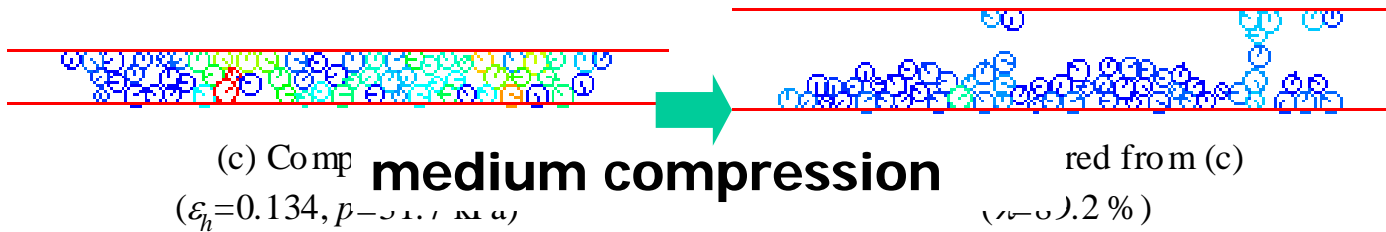
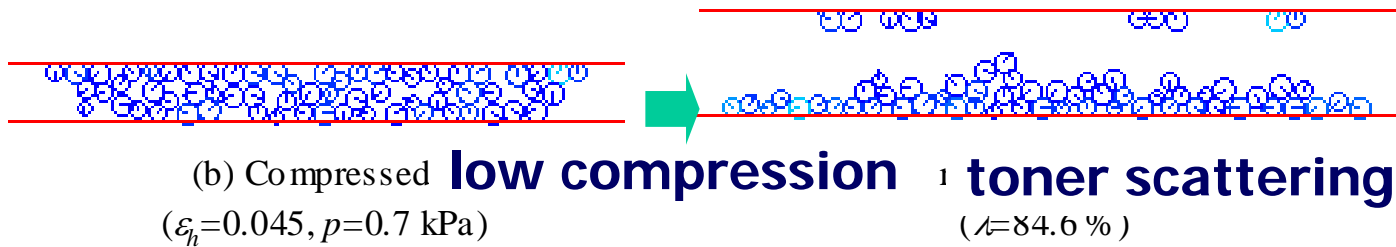
# Hysteresis of Toner Compression



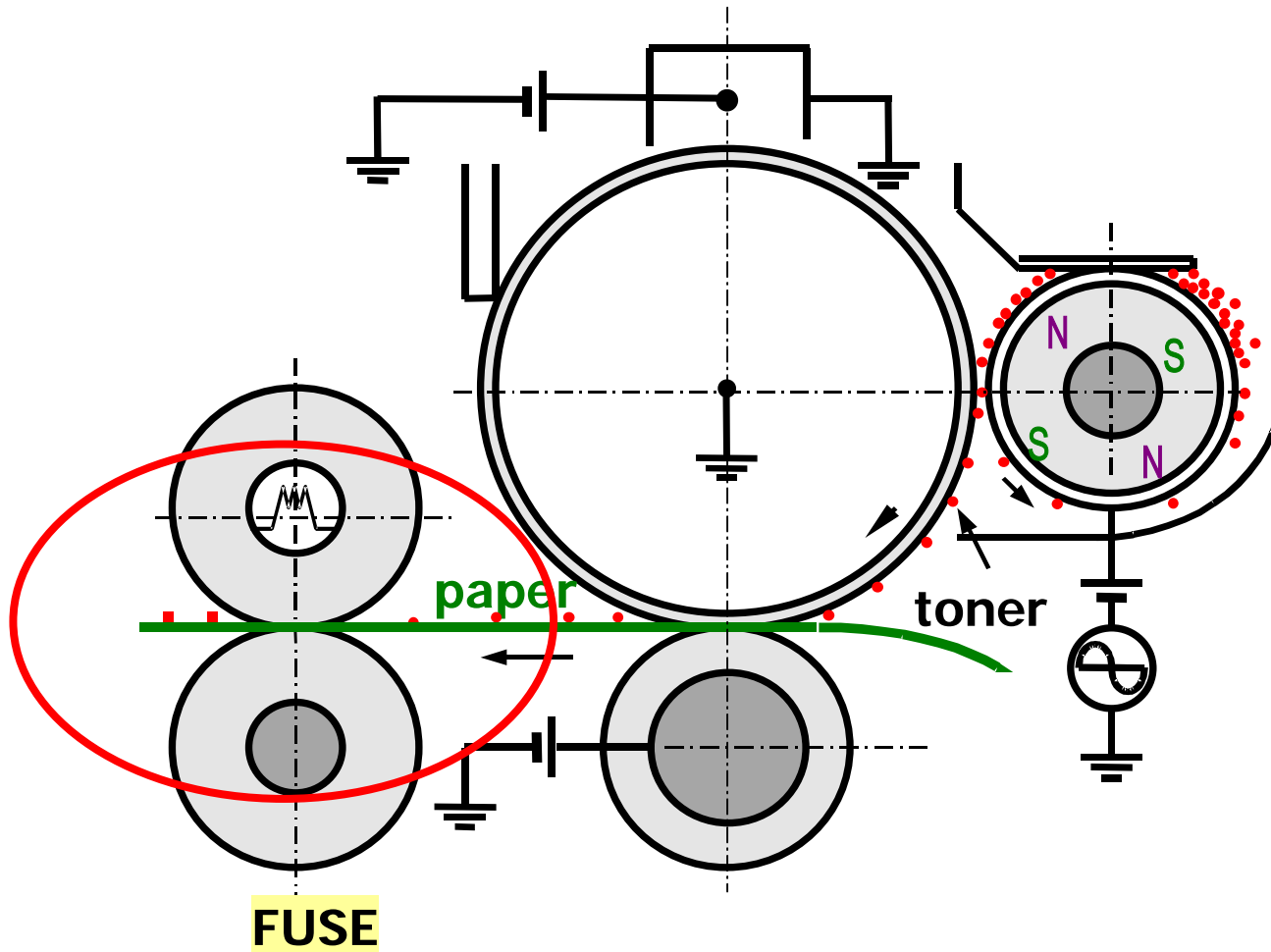
# Hollow Defect and Toner Scattering



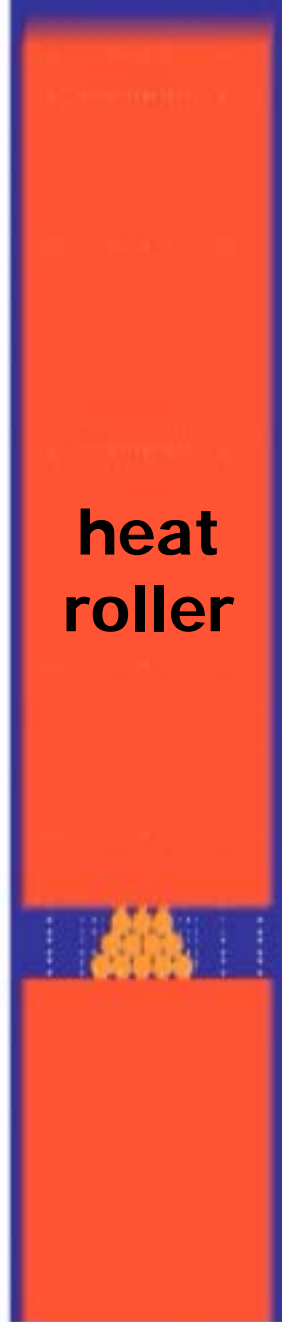
on OPC (before transfer)



# 5. Fusing

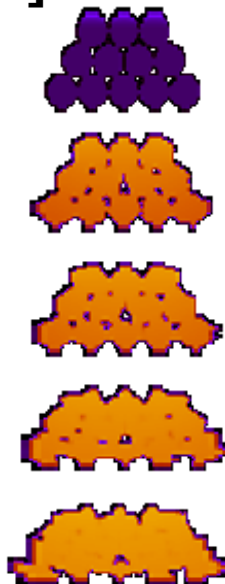
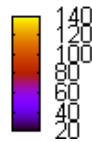


# Visco-Elasticity of Toner



heat  
roller

temp [ ]



Low Fusing Temp.

dwelt time

0 ms



25 ms



35 ms



45 ms

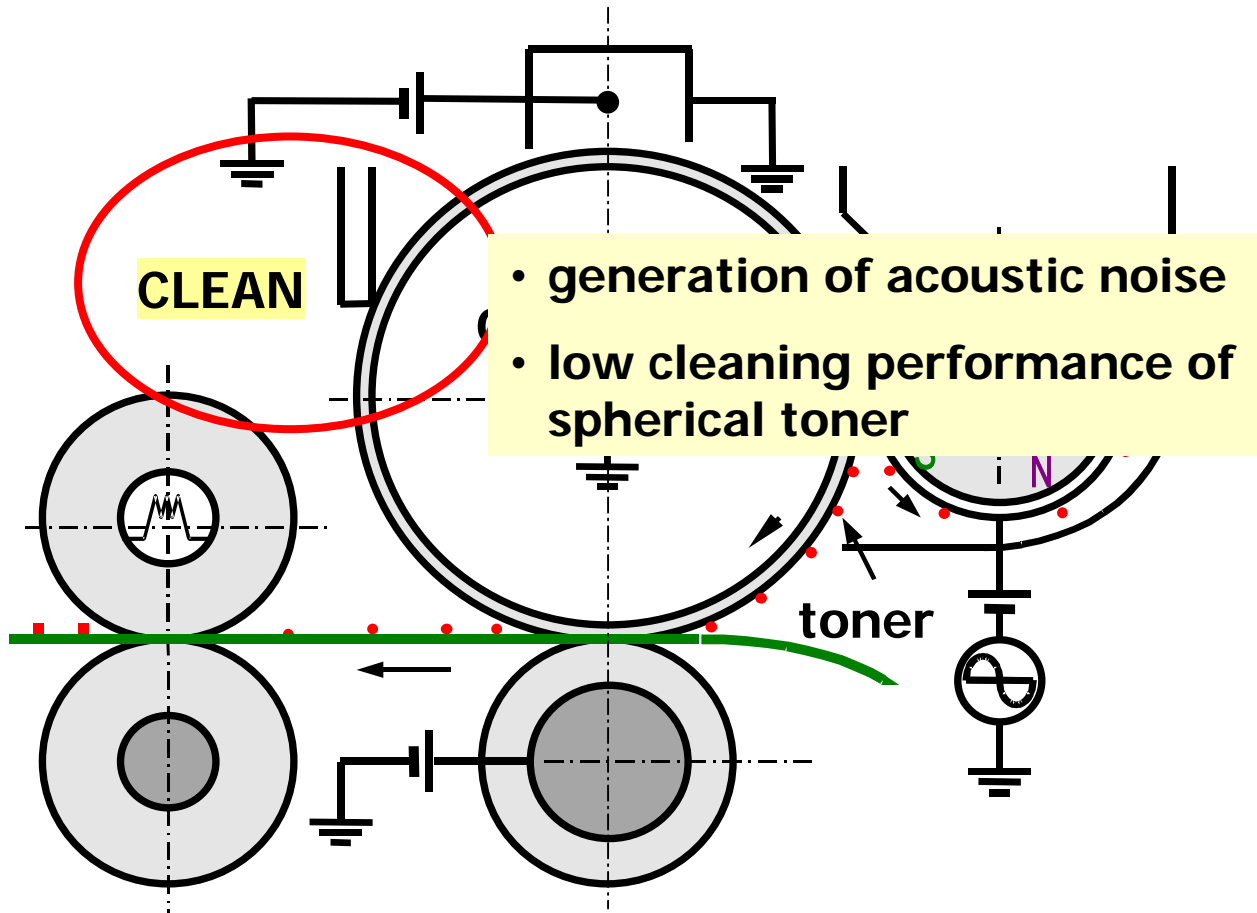


55 ms

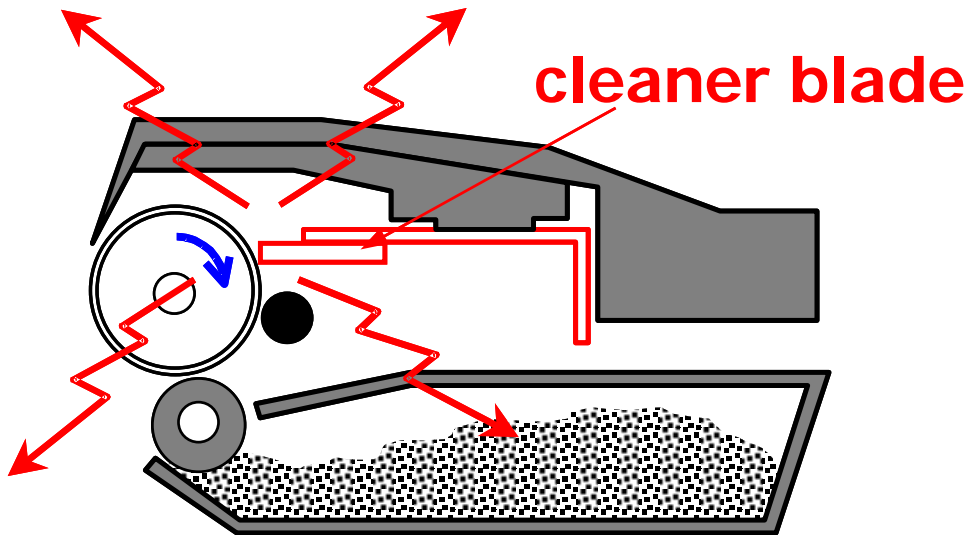


High Fusing Temp.

# 6. Cleaning



# Acoustic Noise from Cleaner Blade



## Low Speed

- **stick-slip**

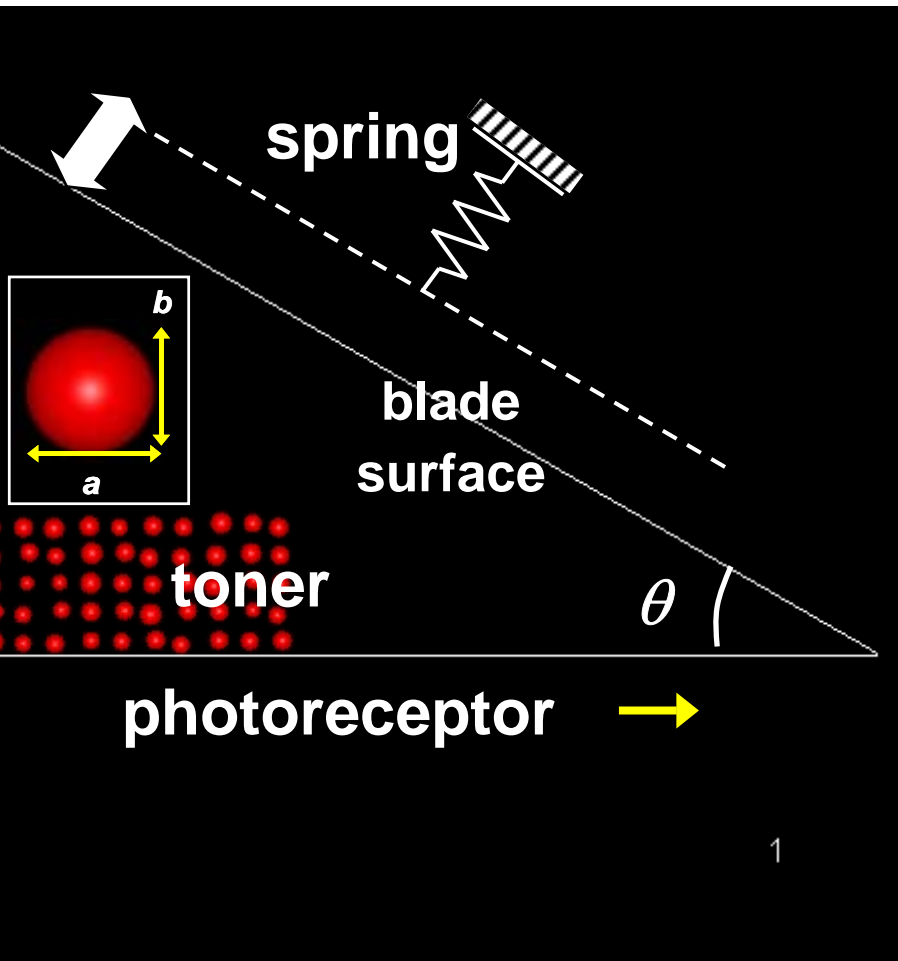
H. Kawamoto (Fuji Xerox) 1995

## Rated Speed

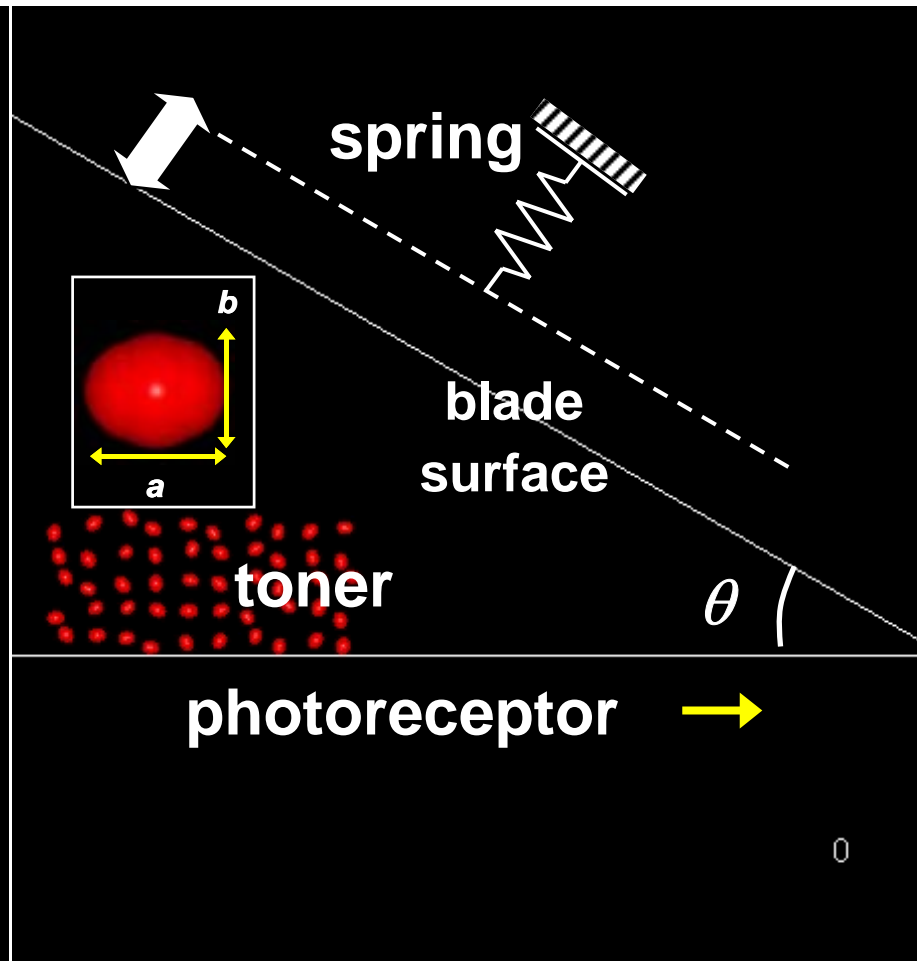
- **coupled non-linear vibration**

M. Kasama (Fuji Xerox) 2006

# Cleaning Performance of Spherical Toner Particles



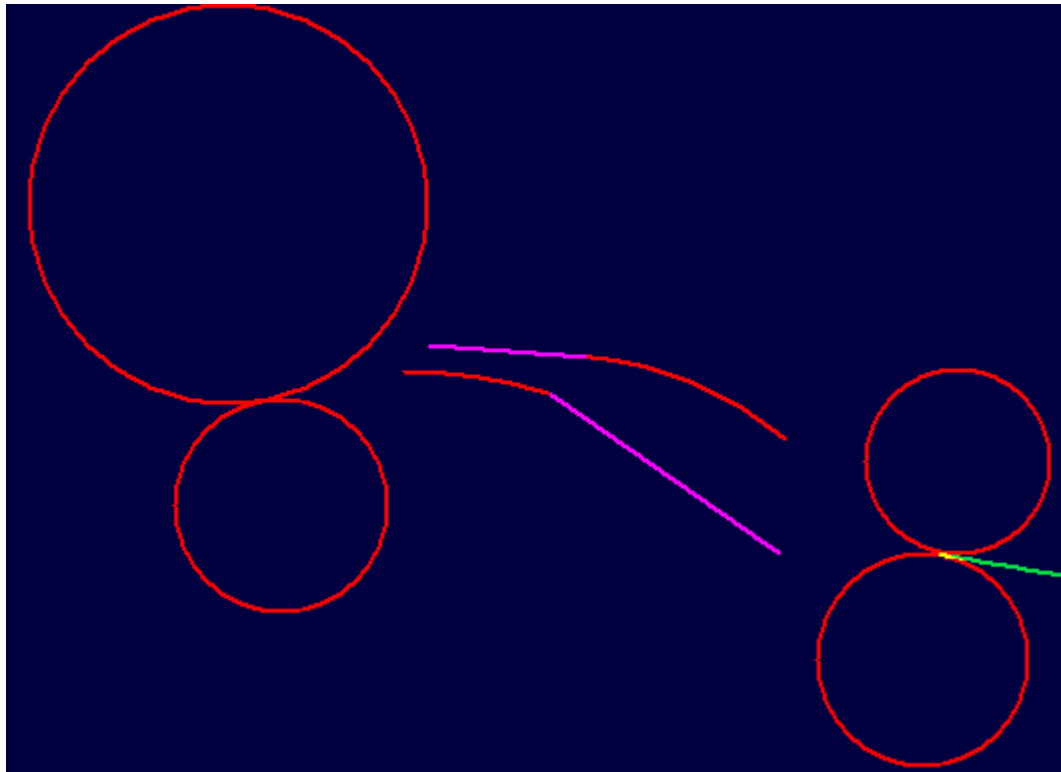
$\mu = 0.96$ ,  $\theta = 30\text{deg}$ ,  $k_w = 10\text{N/m}$ ,  
 $a/b = 1.0$



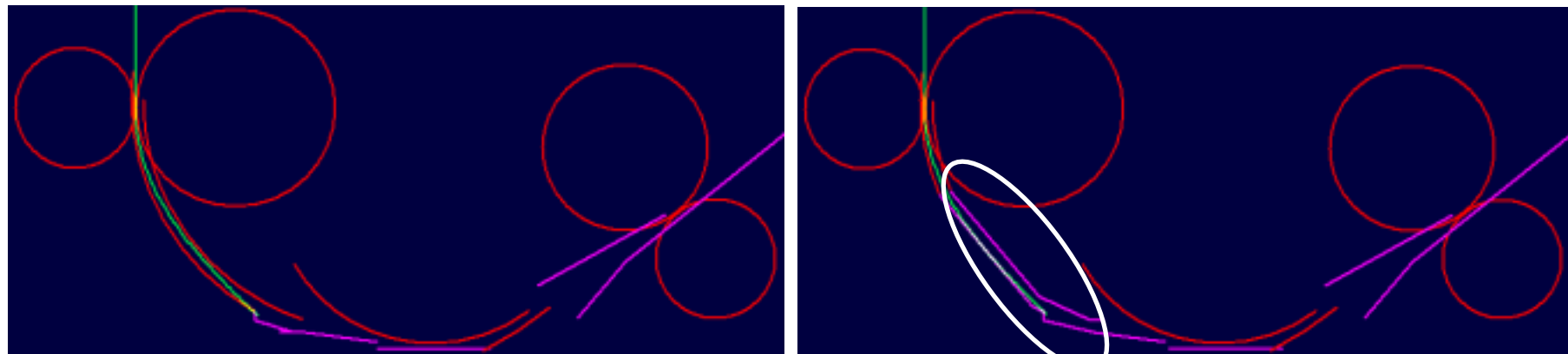
$\mu = 0.96$ ,  $\theta = 30\text{deg}$ ,  $k_w = 10\text{N/m}$ ,  
 $a/b = 1.23$



# 7. Paper Handling



# Improvement of Paper Path for Image Scanner



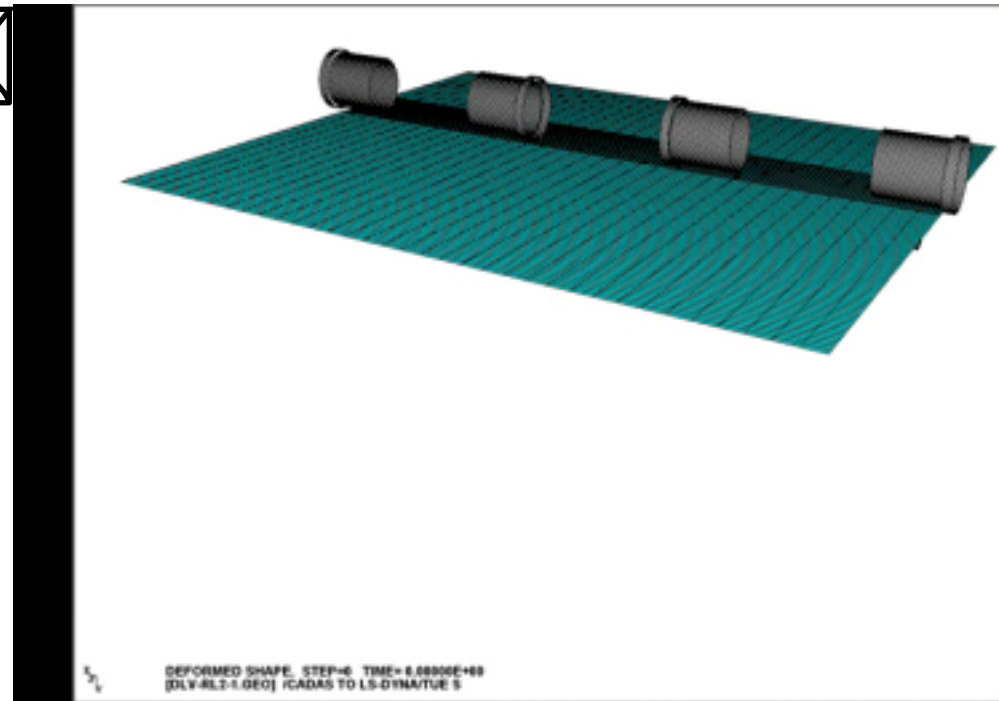
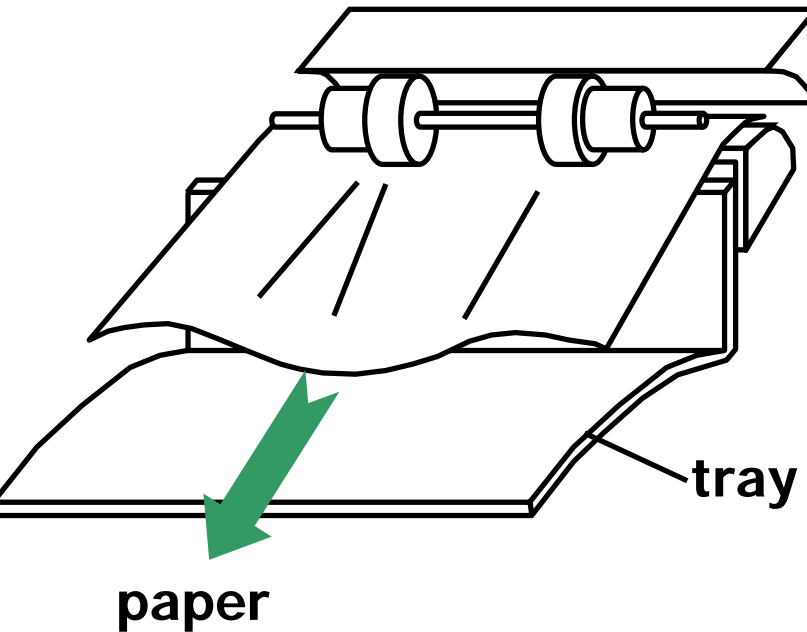
reader ↑

↑ reader

output image



# Application for Paper Feeder



# **Promotion of Simulation Technology and Education of Young Engineers in Japan**

# Academic Committees

Three Japanese academic committees to promote the modeling and numerical simulation of electrophotography processes

- The Imaging Society of Japan (ISJ)
  - education of young engineers
  - publish of textbook
- The Japan Society of Mechanical Engineers (JSME)
  - **technology exchange on a give-and-take basis**
- The Japan Society for Precision Engineering (JSPE)
  - **paper handling**

# Simulation Seminar



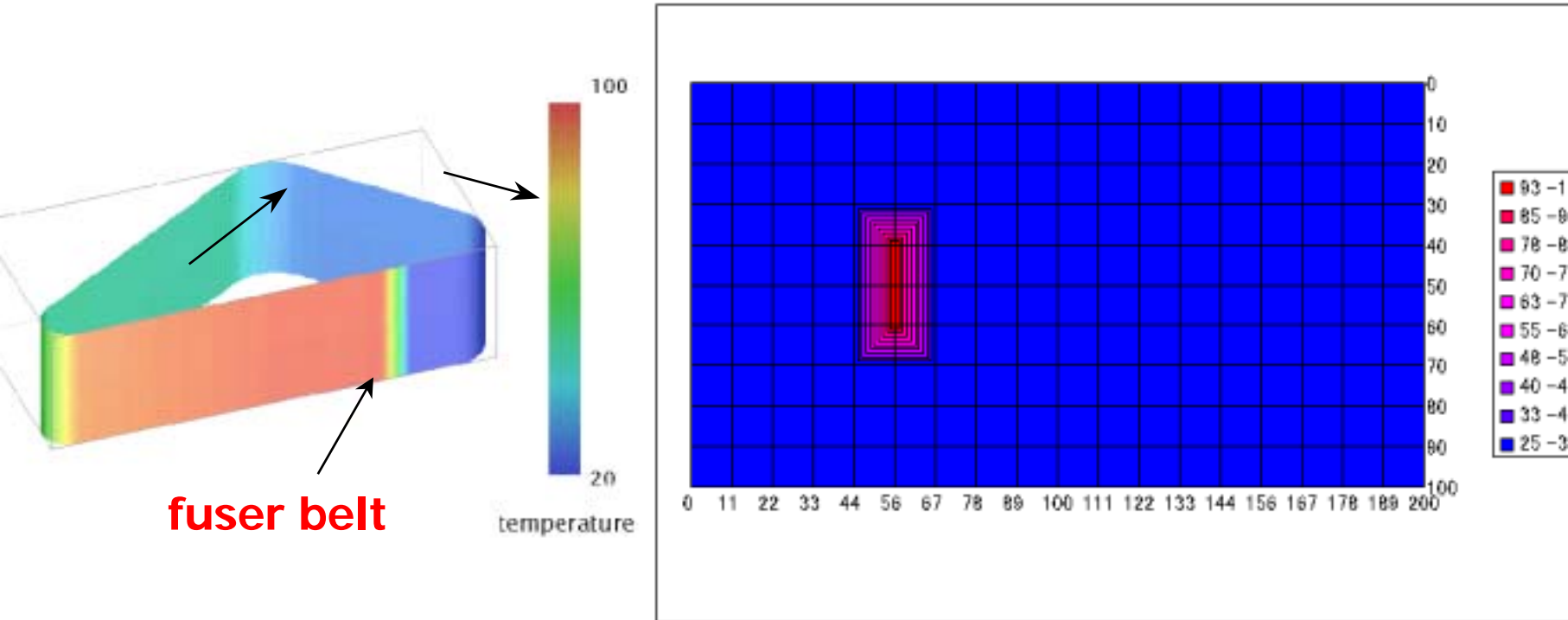
**The seminar is conducted every year for 15 students.**

**Students are young engineers in industries.**

**They do exercise with their own note PC.**

# Example of Exercise

## (Thermal Analysis of Belt Nip Fuser)



**Students must complete the calculation at the end of one-day lecture !!**

# 電子写真

プロセスとシミュレーション

日本画像学会 編

平倉浩治・川本広行 監修

Electrophotography

Process &  
Simulation

Published by The  
Imaging Society of  
Japan

Edited by Hirakura  
(Ricoh) &  
Kawamoto

**Textbook**



# Concluding Remarks

**Simulation technology has been developed and widely utilized for the development of electrophotography machines,**

**although it had been believed that the simulation is ineffective for the electrophotography.**

**The electrophotography processes are no longer a black box.**

# Acknowledgement

**I would like to express my sincere gratitude to my colleagues:**

**Dr. M. Kadonaga (Ricoh)**

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**Mr. O. Takehira (Ricoh)**

**Dr. N. Kuribayashi (Ricoh Printing)**

**Dr. N. Nakayama (Fuji Xerox)**

**Dr. M. Kasama (Fuji Xerox)**

**Dr. T. Ito (Fuji Xerox)**

**Mr. H. Okamoto (Fuji Xerox)**

**Mr. M. Nakano (Canon)**

**Dr. H. Mio (Kyoto Fine Particle Technology)**

**for their beneficial suggestions and discussions.**

# Thank you for your attention.

## For more information

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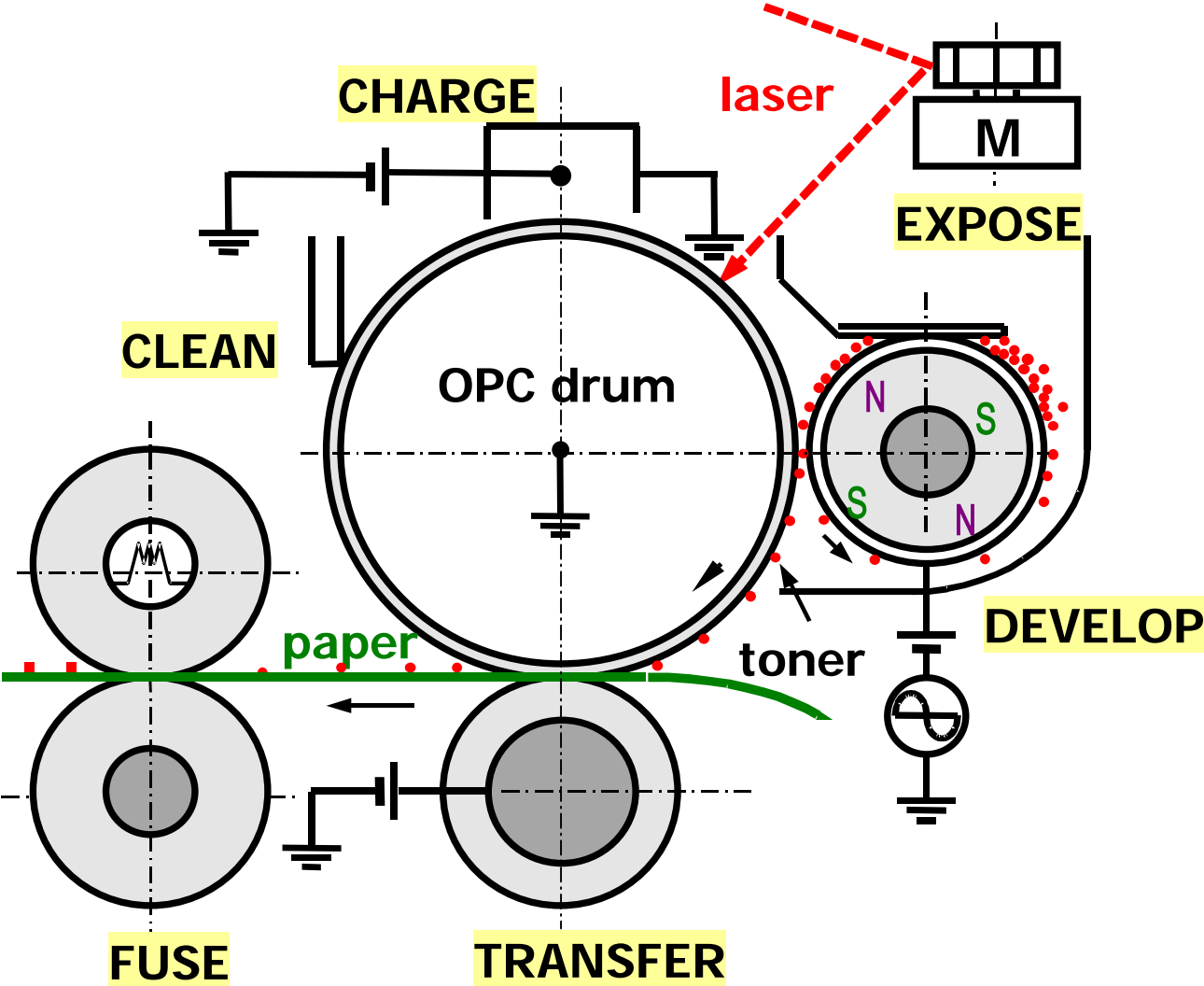
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# Electrophotography Processes



# History of Electrophotography Technology

